SHA-3 proposal BLAKE

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Abstract

BLAKE is our proposal for SHA-3. BLAKE entirely relies on previously analyzed components: it uses the HAIFA iteration mode and builds its compression function on the ChaCha core function. BLAKE resists generic second-preimage attacks, length extension, and side-channel attacks. Theoretical and empirical security guarantees are given, against structural and differential attacks. BLAKE hashes on a Core 2 Duo at 12 cycles/byte, and on a 8-bit PIC microcontroller at 400 cycles/byte. In hardware BLAKE can be implemented in less than 9900 gates, and reaches a throughput of 6 Gbps.

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1 Introduction

In 1993, NIST published the first Secure Hash Standard SHA-0, which two years later was superseded by SHA-1 to fix a flaw in the message expansion. SHA-1 was still deemed secure by the end of the millenium, when researchers' attention turned to block ciphers through the AES competition. Shortly after that, an avalanche of results on hash functions culminated with collision attacks for MD5 and SHA-1, while in the meantime NIST had introduced the SHA-2 family, unbroken until now. But attacks on SHA-1 arguably raise doubts on the long-term security of SHA-2, because of its very similar structure. In response NIST announced the SHA-3 program, calling for proposals for a hash function that will augment the SHA-2 standard. Many recent results illustrate the obsolescence of designs based on MD5 and SHA-1: only in the first semester of 2008, were published new collision attacks for (reduced) SHA-256 [33] and the first preimage attacks for (reduced) MD5 [4], SHA-0, and SHA-1 [21].

BLAKE is our candidate for SHA-3. It meets all the criteria set by NIST, offers theoretical and empirical security guarantees, and performs well from high-end PC's to light hardware. We did not reinvent the wheel; BLAKE is built on previously studied components, chosen for their complementarity. The heritage of BLAKE is threefold:

- its iteration mode is HAIFA, an improved version of the Merkle-Damgård paradigm proposed by Biham and Dunkelman. It provides resistance to long-message second preimage attacks, and explicitly handles hashing with a salt.
- its **internal structure** is the local wide-pipe, which we already used with the LAKE hash function. It makes local collisions impossible in the BLAKE hash functions, a result that doesn't rely on any intractability assumption.
- its **compression algorithm** is a modified version of Bernstein's stream cipher ChaCha, whose security has been intensively analyzed and performance is excellent, and which is strongly parallelizable.

The iteration mode HAIFA would significantly benefit to the new hash standard, for it provides randomized hashing and structural resistance to second-preimage attacks. The LAKE local wide-pipe structure is a straightforward way to give strong security guarantees against collision attacks. Finally, the choice of borrowing from the stream cipher ChaCha (after agreement of its author) comes from our experience in cryptanalysis of Salsa20 and ChaCha [3], when we got convinced of their remarkable combination of simplicity and security.

Content of this document: The present chapter contains design principles, a short description of BLAKE, and security claims. Chapter 2 gives a complete specification of the BLAKE hash functions. Chapter 3 reports performance in FPGA, ASIC, 8-bit microcontroller, and 32-and 64-bit processor. Chapter 4 explains how to use BLAKE, detailing construction of HMAC, UMAC, and PRF ensembles. Chapter 5 gives elements of analysis, including attacks on simplified versions. We conclude with acknowledgments, references, and appendices containing source code and intermediate values.

1.1 Design principles

The BLAKE hash functions were designed to meet all NIST criteria for SHA-3, including:

- message digests of 224, 256, 384, and 512 bits
- same parameter sizes as SHA-2
- one-pass streaming mode
- maximum message length of at least $2^{64} 1$ bits

In addition, we imposed BLAKE to:

- · explicitly handle hashing with a salt
- be parallelizable
- allow performance trade-offs
- be suitable for lightweight environments

We briefly justify these choices: First, a built-in salt simplifies a lot of things; it provides an interface for an extra input, avoids insecure homemade modes, and encourages the use of randomized hashing. Parallelism is a big advantage for hardware implementations, which can also be exploited by certain large microprocessors. In addition, BLAKE allows a trade-off throughput/area to adapt the implementation to the hardware available.

Oppositely, we excluded the following goals:

- have a reduction to a supposedly hard problem
- have homomorphic or incremental properties
- have a scalable design
- have a specification for variable length hashing

We justify these choices: The relative unsuccess of provably secure hash functions stresses the limitations of the approach: though of theoretical interest, such designs tend to be inefficient, and their highly structured constructions expose them to attacks with respect to notions other than the proved one. The few advantages of homomorphic and incremental hash functions are not worth their cost; more importantly, these properties are undesirable in many applications. Scalability of the design to various parameter sizes has no real advantage in practice, and the security of scalable designs is difficult to assess. Finally, we deemed unnecessary to complicate the function with variable-length features; in practice users can just truncate the hash values for shorter hashes, and there is no demand for hash values of more than 512 bits.

To summarize, we made our candidate as simple as possible, and combined well-known and trustable building blocks so that BLAKE already looks familiar to cryptanalysts. We avoided any show-off feature, and just provide what users really need or will need in a close future (like hashing with a salt). It was essential for us to build on previous knowledge—be it about security or implementation—in order to adapt our proposal to the low resources available for analyzing the SHA-3 candidates.

1.2 BLAKE in a nutshell

BLAKE is a family of four hash functions: BLAKE-28, BLAKE-32, BLAKE-48, and BLAKE-64 (see Table 1.1). As with SHA-2, we have a 32-bit version (BLAKE-32) and a 64-bit one (BLAKE-64), from which other instances are derived using different initial values, different padding, and truncated output.

Algorithm	Word	Message	Block	Digest	Salt
BLAKE-28	32	$< 2^{64}$	512	224	128
BLAKE-32	32	$< 2^{64}$	512	256	128
BLAKE-48	64	<2 ¹²⁸	1024	384	256
BLAKE-64	64	$< 2^{128}$	1024	512	256

Table 1.1: Properties of the BLAKE hash functions (sizes in bits).

The BLAKE hash functions follow the HAIFA iteration mode [10]: the compression function depends on a *salt*¹ and the *number of bits hashed so far* (counter), to compress each message block with a distinct function. The structure of BLAKE's compression function is inherited from LAKE [5] (see Fig. 1.1): a large inner state is initialized from the initial value, the salt, and the counter. Then it is injectively updated by message-dependent *rounds*, and it is finally compressed to return the next chain value. This strategy was called *local wide-pipe* in [5], and is inspired by the wide-pipe iteration mode [30].

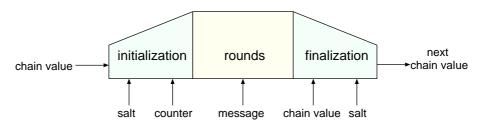


Figure 1.1: The local wide-pipe construction of BLAKE's compression function.

The inner state of the compression function is represented as a 4×4 matrix of words. A round of BLAKE-32 is a modified "double-round" of the stream cipher ChaCha: first, all four columns are updated independently, and thereafter four disjoint diagonals. In the update of each column or diagonal, two message words are input according to a round-dependent permutation. Each round is parametrized by distinct constants to minimize self-similarity. After the sequence of rounds, the state is reduced to half its length with feedforward of the initial value and the salt.

An implementation of BLAKE requires low resources, and is fast in both software and hardware environments. BLAKE can be implemented in hardware in less than 9 900 gates, and reach a throughput of 6 Gbps. In a 8-bit PIC microcontroller, BLAKE hashes at 400 cycles/byte; on our 32-bit Celeron at 22 cycles/byte, and on our 64-bit Core 2 Duo at 12 cycles/byte.

¹A value that parametrizes the function, and can be either public or secret.

1.3 Expected strength

For all BLAKE hash functions, there should be no attack significantly more efficient than standard bruteforce methods for

- finding collisions, with same or distinct salt
- finding (second) preimages, with arbitrary salt

BLAKE should also be secure for randomized hashing, with respect to the experiment described by NIST in [36, 4.A.ii]. It should be impossible to distinguish a BLAKE instance with an unknown salt (that is, uniformly chosen at random) from a PRF, given blackbox access to the function; more precisely, it shouldn't cost significantly less than $2^{|s|}$ queries to the box, where |s| is the bit length of the salt. BLAKE should have no property that makes its use significantly less secure than an ideal function for any concrete application. (These claims concern the proposed functions with the *recommended* number of rounds, not reduced or modified versions.)

1.4 Advantages and limitations

We summarize the advantages and limitations of BLAKE:

Advantages

Design

- simplicity of the algorithm
- interface for hashing with a salt

Performance

- fast in both software and hardware
- parallelism and throughput/area trade-off for hardware implementation
- simple speed/confidence trade-off with the tunable number of rounds

Security

- based on an intensively analyzed component (ChaCha)
- resistant to generic second-preimage attacks
- resistant to side-channel attacks
- · resistant to length-extension

Limitations

- message length limited to respectively 2⁶⁴ and 2¹²⁸ for BLAKE-32 and BLAKE-64
- resistance to Joux's multicollisions similar to that of SHA-2
- fixed-points found in less time than for an ideal function (but not efficiently)

1.5 Notations

Hexadecimal numbers are written in typewriter style (for example F0 = 240). A *word* is either a 32-bit or a 64-bit string, depending on the context. We use the same conventions of bigendianness as NIST does in the SHA-2 specification [34, $\S 3$]. In particular, we use (unsigned) big-endian representation for expressing integers, and, e.g. converting data streams into word arrays. Table 1.2 summarizes the basic operations used.

Symbol	Meaning
— ← + ⊕	variable assignment addition modulo 2^{32} or (modulo 2^{64}) Boolean exclusive OR (XOR)
$\gg k$ $\ll k$ $\langle \ell \rangle_k$	rotation of k bits towards less significant bits rotation of k bits towards more significant bits encoding of the integer ℓ over k bits

Table 1.2: Operations symbols used in this document.

If p is a bit string, we view it as a sequence of words and p_i denotes its i^{th} word component; thus $p = p^0 \| p^1 \| \dots$ For a message m, m^i denotes its i^{th} 16-word block, thus m^i_j is the j^{th} word of the i^{th} block of m. Indices start from zero, for example a N-block message m is decomposed as $m = m^0 m^1 \dots m^{N-1}$, and the block m^0 is composed of words $m^0_0, m^0_1, m^0_2, \dots, m^0_{15}$,

The adjective *random* here means uniformly random with respect to the relevant probability space. For example a "random salt" of BLAKE-32 is a random variable uniformly distributed over {0, 1}¹²⁸, and may also mean "uniformly chosen at random". The *initial value* is written IV; intermediate hash values in the iterated hash are called *chain values*, and the last one is the *hash value*, or just *hash*.

2 Specification

This chapter defines the hash functions BLAKE-32, BLAKE-64, BLAKE-28, and BLAKE-48.

2.1 BLAKE-32

The hash function BLAKE-32 operates on 32-bit words and returns a 32-byte hash value. This section defines BLAKE-32, going from its constant parameters to its compression function, then to its iteration mode.

2.1.1 Constants

BLAKE-32 starts hashing from the same initial value as SHA-256:

$IV_0 = 6A09E667$	$IV_1 = BB67AE85$
$IV_2 = 3C6EF372$	$IV_3 = \mathtt{A54FF53A}$
$IV_4 = 510E527F$	$IV_5 = 9B05688C$
$IV_6 = 1F83D9AB$	$IV_7 = 5BE0CD19$

BLAKE-32 uses 16 constants¹

Ten permutations of $\{0, \dots, 15\}$ are used by all BLAKE functions, defined in Table 2.1.

2.1.2 Compression function

The compression function of BLAKE-32 takes as input four values:

- a chain value h = h₀,..., h₇
- a message block $m = m_0, \dots, m_{15}$
- a salt $s = s_0, ..., s_3$
- a counter $t = t_0, t_1$

 $^{^{1}}$ First digits of π .

σ_0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
σ_1	14	10	4	8	9	15	13	6	1	12	0	2	11	7	5	3
σ_2	11	8	12	0	5	2	15	13	10	14	3	6	7	1	9	4
σ_3	7	9	3	1	13	12	11	14	2	6	5	10	4	0	15	8
σ4	9	0	5	7	2	4	10	15	14	1	11	12	6	8	3	13
σ_5	2	12	6	10	0	11	8	3	4	13	7	5	15	14	1	9
σ_6	12	5	1	15	14	13	4	10	0	7	6	3	9	2	8	11
σ_7	13	11	7	14	12	1	3	9	5	0	15	4	8	6	2	10
σ_8	6	15	14	9	11	3	0	8	12	2	13	7	1	4	10	5
σ9	10	2	8	4	7	6	1	5	15	11	9	14	3	12	13	0

Table 2.1: Permutations of $\{0, ..., 15\}$ used by the BLAKE functions.

These four inputs represent 30 words in total (i.e., 120 bytes = 960 bits). The output of the function is a new chain value $h' = h'_0, \dots, h'_7$ of eight words (i.e., 32 bytes = 256 bits). We write the compression of h, m, s, t to h' as

$$h' = compress(h, m, s, t)$$

Initialization

A 16-word state v_0, \dots, v_{15} is initialized such that different inputs produce different initial states. The state is represented as a 4×4 matrix, and filled as follows:

$$\begin{pmatrix} v_0 & v_1 & v_2 & v_3 \\ v_4 & v_5 & v_6 & v_7 \\ v_8 & v_9 & v_{10} & v_{11} \\ v_{12} & v_{13} & v_{14} & v_{15} \end{pmatrix} \leftarrow \begin{pmatrix} h_0 & h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 & h_7 \\ s_0 \oplus c_0 & s_1 \oplus c_1 & s_2 \oplus c_2 & s_3 \oplus c_3 \\ t_0 \oplus c_4 & t_0 \oplus c_5 & t_1 \oplus c_6 & t_1 \oplus c_7 \end{pmatrix}$$

Round function

Once the state ν is initialized, the compression function iterates a series of 10 rounds. A round is a transformation of the state ν , which computes

where, at round r, $G_i(a, b, c, d)$ sets²

$$\begin{array}{lll} a & \leftarrow & a+b+(m_{\sigma_r(2i)}\oplus c_{\sigma_r(2i+1)}) \\ d & \leftarrow & (d\oplus\alpha) \ggg 16 \\ c & \leftarrow & c+d \\ b & \leftarrow & (b\oplus c) \ggg 12 \\ a & \leftarrow & a+b+(m_{\sigma_r(2i+1)}\oplus c_{\sigma_r(2i)}) \\ d & \leftarrow & (d\oplus\alpha) \ggg 8 \\ c & \leftarrow & c+d \\ b & \leftarrow & (b\oplus c) \ggg 7 \end{array}$$

 $^{^2}$ In the rest of the paper, for statements that don't depend on the index i we shall omit the subscript and write simply G.

The first four calls G_0, \ldots, G_3 can be computed in parallel, because each of them updates a distinct column of the matrix. We call the procedure of computing G_0, \ldots, G_3 a column step. Similarly, the last four calls G_4, \ldots, G_7 update distinct diagonals thus can be parallelized as well, which we call a diagonal step.

Figures 2.1 and 2.2 illustrate G_i , the column step, and the diagonal step. An example of computation is given in Appendix A.

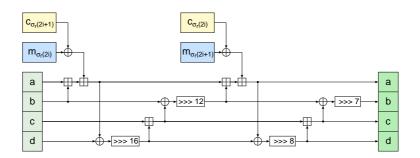


Figure 2.1: The G_i function.

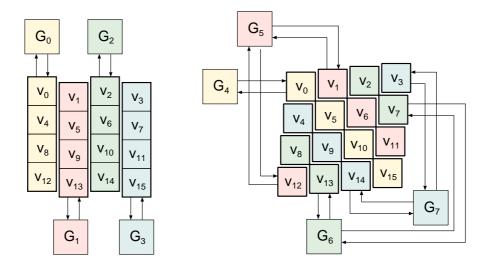


Figure 2.2: Column step and diagonal step.

Finalization

After the rounds sequence, the new chain value h'_0, \ldots, h'_7 is extracted from the state v_0, \ldots, v_{15} with input of the initial chain value h_0, \ldots, h_7 and the salt s_0, \ldots, s_3 :

$$\begin{array}{lll} h_0' & \leftarrow & h_0 \oplus s_0 \oplus \nu_0 \oplus \nu_8 \\ h_1' & \leftarrow & h_1 \oplus s_1 \oplus \nu_1 \oplus \nu_9 \\ h_2' & \leftarrow & h_2 \oplus s_2 \oplus \nu_2 \oplus \nu_{10} \\ h_3' & \leftarrow & h_3 \oplus s_3 \oplus \nu_3 \oplus \nu_{11} \\ h_4' & \leftarrow & h_4 \oplus s_0 \oplus \nu_4 \oplus \nu_{12} \\ h_5' & \leftarrow & h_5 \oplus s_1 \oplus \nu_5 \oplus \nu_{13} \\ h_6' & \leftarrow & h_6 \oplus s_2 \oplus \nu_6 \oplus \nu_{14} \\ h_7' & \leftarrow & h_7 \oplus s_3 \oplus \nu_7 \oplus \nu_{15} \end{array}$$

2.1.3 Hashing a message

We now describe the procedure for hashing a message \mathfrak{m} of bit length $\ell < 2^{64}$. As it is usual for iterated hash functions, the message is first *padded* (BLAKE uses a padding rule very similar to that of HAIFA), then it is processed block per block by the compression function.

Padding

First the message is extended so that its length is congruent to 447 modulo 512. Length extension is performed by appending a bit 1 followed by a sufficient number of 0 bits. At least one bit and at most 512 are appended. Then a bit 1 is added, followed by a 64-bit unsigned big-endian representation of ℓ . Padding can be represented as

$$m \leftarrow m \| 1000 \dots 0001 \langle \ell \rangle_{64}$$

This procedure guarantees that the bit length of the padded message is a multiple of 512.

Iterated hash

To proceed to the iterated hash, the padded message is split into 16-word blocks $\mathfrak{m}^0,\ldots,\mathfrak{m}^{N-1}$. We let ℓ^i be the number of message bits in $\mathfrak{m}^0,\ldots,\mathfrak{m}^i$, that is, excluding the bits added by the padding. For example, if the original (non-padded) message is 600-bit long, then the padded message has two blocks, and $\ell^0=512,\ \ell^1=600$. A particular case occurs when the last block contains *no original message bit*, for example a 1020-bit message leads to a padded message with three blocks (which contain respectively 512, 508, and 0 message bits), and we set $\ell^0=512,\ \ell^1=1020,\ \ell^2=0$. The general rule is: if the last block contains no bit from the original message, then the counter is set to zero; this guarantees that if $\mathfrak{i}\neq\mathfrak{j}$, then $\ell_\mathfrak{i}\neq\ell_\mathfrak{j}$.

The salt s is chosen by the user, and set to the null value when no salt is required (i.e., $s_0 = s_1 = s_2 = s_3 = 0$). The hash of the padded message m is then computed as follows:

The procedure of hashing $\mathfrak m$ with BLAKE-32 is aliased BLAKE-32($\mathfrak m,s$) = $\mathfrak h^N$, where $\mathfrak m$ is the (non-padded) message, and s is the salt. The notation BLAKE-32($\mathfrak m$) denotes the hash of $\mathfrak m$ when no salt is used (i.e., s=0).

2.2 BLAKE-64

BLAKE-64 operates on 64-bit words and returns a 64-byte hash value. All lengths of variables are doubled compared to BLAKE-32: chain values are 512-bit, message blocks are 1024-bit, salt is 256-bit, counter is 128-bit.

2.2.1 Constants

The initial value of BLAKE-64 is the same as for SHA-512:

$IV_0 = 6A09E667F3BCC908$	$IV_1 = BB67AE8584CAA73B$
$IV_2 = 3C6EF372FE94F82B$	$IV_3 = \mathtt{A54FF53A5F1D36F1}$
$IV_4 = 510E527FADE682D1$	$IV_5 = 9B05688C2B3E6C1F$
$IV_6 = 1F83D9ABFB41BD6B$	$IV_7 = 5BE0CD19137E2179$

BLAKE-64 uses the constants³

$c_0 = 243F6A8885A308D3$	$c_1 = 13198A2E03707344$
$c_2 = A4093822299F31D0$	$c_3 = 082$ EFA98EC4E6C89
$c_4 = 452821E638D01377$	$c_5 = \mathtt{BE5466CF34E90C6C}$
$c_6 = \texttt{COAC29B7C97C50DD}$	$c_7 = 3F84D5B5B5470917$
$c_8 = 9216D5D98979FB1B$	$c_9 = D1310BA698DFB5AC$
$c_{10} = 2FFD72DBD01ADFB7$	$c_{11} = B8E1AFED6A267E96$
$c_{12} = BA7C9045F12C7F99$	$c_{13} = 24A19947B3916CF7$
$c_{14} = 0801F2E2858EFC16$	$c_{15} = 636920D871574E69$

Permutations are the same as for BLAKE-32 (see Table 2.1).

2.2.2 Compression function

The compression function of BLAKE-64 is similar to that of BLAKE-32 except that it makes 14 rounds instead of 10, and that $G_i(a,b,c,d)$ computes

```
\begin{array}{lll} \boldsymbol{a} & \leftarrow & \boldsymbol{a} + \boldsymbol{b} + (\boldsymbol{m}_{\sigma_r(2i)} \oplus \boldsymbol{c}_{\sigma_r(2i+1)}) \\ \boldsymbol{d} & \leftarrow & (\boldsymbol{d} \oplus \boldsymbol{a}) \ggg 32 \\ \boldsymbol{c} & \leftarrow & \boldsymbol{c} + \boldsymbol{d} \\ \boldsymbol{b} & \leftarrow & (\boldsymbol{b} \oplus \boldsymbol{c}) \ggg 25 \\ \boldsymbol{a} & \leftarrow & \boldsymbol{a} + \boldsymbol{b} + (\boldsymbol{m}_{\sigma_r(2i+1)} \oplus \boldsymbol{c}_{\sigma_r(2i)}) \\ \boldsymbol{d} & \leftarrow & (\boldsymbol{d} \oplus \boldsymbol{a}) \ggg 16 \\ \boldsymbol{c} & \leftarrow & \boldsymbol{c} + \boldsymbol{d} \\ \boldsymbol{b} & \leftarrow & (\boldsymbol{b} \oplus \boldsymbol{c}) \ggg 11 \end{array}
```

The only differences with BLAKE-32's G_i are the word length (64 bits instead of 32) and the rotation distances. At round r>9, the permutation used is $\sigma_{r \bmod 10}$ (for example, in the last round r=13 and the permutation $\sigma_{13 \bmod 10}=\sigma_3$ is used).

 $^{^3}$ First digits of π .

2.2.3 Hashing a message

For BLAKE-64, message padding goes as follows: append a bit 1 and as many 0 bits until the message bit length is congruent to 895 modulo 1024. Then append a bit 1, and a 128-bit unsigned big-endian representation of the message bit length:

$$m \leftarrow m \| 1000 \dots 0001 \langle \ell \rangle_{128}$$

This procedure guarantees that the length of the padded message is a multiple of 1024. The algorithm for iterated hash is identical to that of BLAKE-32.

2.3 BLAKE-28

BLAKE-28 is similar to BLAKE-32, except that

• it uses the initial value of SHA-224:

$IV_0 = C1059ED8$	$IV_1 = 367CD507$
$IV_2 = 3070DD17$	$IV_3 = F70E5939$
$IV_4 = FFC00B31$	$IV_5 = 68581511$
$IV_6 = 64F98FA7$	$IV_7 = \mathtt{BEFA4FA4}$

• in the padded data, the 1 bit preceeding the message length is replaced by a 0 bit:

$$m \leftarrow m \| 1000 \dots 0000 \langle \ell \rangle_{64}$$

• the output is truncated to its first 224 bits, that is, the iterated hash returns h_0^N,\ldots,h_6^N instead of $h^N=h_0^N,\ldots,h_7^N$

2.4 BLAKE-48

BLAKE-48 is similar to BLAKE-64, except that

• it uses the initial value of SHA-384:

$IV_0 = CBBB9D5DC1059ED8$	$IV_1 = 629A292A367CD507$
$IV_2 = 9159015A3070DD17$	$IV_3 = 152FECD8F70E5939$
$IV_4 = 67332667FFC00B31$	$IV_5 = \mathtt{8EB44A8768581511}$
$IV_6 = \mathtt{DBOC2E0D64F98FA7}$	$IV_7 = 47B5481DBEFA4FA4$

in the padded data, the 1 bit preceding the message length is replaced by a 0 bit:

$$m \leftarrow m \| 1000 \dots 0000 \langle \ell \rangle_{128}$$

• the output is truncated to its first 384 bits, that is, the iterated hash returns h_0^N,\dots,h_5^N instead of $h^N=h_0^N,\dots,h_7^N$

2.5 Alternative descriptions

The round function of BLAKE described in §2.1.2 operates first on columns of the matrix state, second on diagonals (see Fig. 2.2). Another way to view this transformation is

- 1. make a column-step
- 2. rotate the i^{th} column up by i positions, for $i = 0, \dots, 3$
- 3. make a row-step (see Fig. 2.3), that is,

$$G_4(v_0, v_1, v_2, v_3)$$
 $G_5(v_4, v_5, v_6, v_7)$ $G_6(v_8, v_9, v_{10}, v_{11})$ $G_7(v_{12}, v_{13}, v_{14}, v_{15})$

A similar description was used for the stream cipher Salsa20 [9].

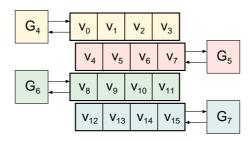


Figure 2.3: Row step of the alternative description.

Similarly, the transformation could be viewed as follows:

- 1. make a column-step
- 2. rotate the i^{th} row by i positions left, for $i = 0, \dots, 3$
- 3. make a column-step again

Finally, another equivalent definition of a round is

where $G_i(a, b, c, d)$ is redefined to

$$\begin{array}{lll} a & \leftarrow & a+b+(m_{\sigma_r(i)}\oplus c_{\sigma_r(i+1)}) \\ d & \leftarrow & (d\oplus a) \ggg 16 \\ c & \leftarrow & c+d \\ b & \leftarrow & (b\oplus c) \ggg 12 \\ a & \leftarrow & a+b+(m_{\sigma_r(i+1)}\oplus c_{\sigma_r(i)}) \\ d & \leftarrow & (d\oplus a) \ggg 8 \\ c & \leftarrow & c+d \\ b & \leftarrow & (b\oplus c) \ggg 7 \end{array}$$

This definition may speed up implementations by saving the doublings.

2.6 Tunable parameter

In its call for a new hash function [36], NIST encourages the description of a parameter that allows speed/confidence trade-offs. For BLAKE this parameter is the *number of rounds*. We estimate that 5 rounds are a minimum for BLAKE-32 (and BLAKE-28), and we recommend 10 rounds. For BLAKE-64 (and BLAKE-48), 7 rounds are a minimum and we recommend 14 rounds. Rationales behind these choices appear in Chapter 5.

3 Performance

We implemented BLAKE in several environments (software and hardware). This chapter reports results from our implementations.

3.1 Generalities

This section gives general facts about the complexity of BLAKE, independently of any implementation.

3.1.1 Complexity

Number of operations

A single G makes 6 XOR's, 6 additions and 4 rotations, so 16 arithmetic operations in total¹. Hence a round makes 48 XOR's, 48 additions and 32 rotations, so 128 operations. BLAKE-32's compression function thus counts 480 XOR's, 480 additions, 320 rotations, plus 4 XOR's for the initialization and 24 XOR's for the finalization, thus a total of 1312 operations. BLAKE-64's compression function counts 672 XOR's, 672 additions, 448 rotations, plus 4 XOR's and 24 XOR's, thus a total of 1824 operations. We omit the overhead for initializing the hash structure, padding the message, etc., whose cost is negligible compared to that of a compression function.

Memory

BLAKE-32 needs to store in ROM 64 bytes for the constants, and 80 bytes to describe the permutations (144 bytes in total). In RAM, the storage m,h,s,t and ν requires 184 bytes. In practice, however, more space might be required. For example, our implementation on the PIC18F2525 microcontroller (see §3.3) stores the 8-bit addresses of the permutation elements, not the 4-bit elements directly, thus using 160 bytes for storing the 80 bytes of information of the message permutations.

3.1.2 Memory/speed tradeoffs

A memory/speed tradeoff for a hash function implementation consists in storing a larger amount of data, in order to reduce the number of computation steps. This is relevant, for example, for hash functions that use a a large set of constants generated from a smaller set of constants. BLAKE, however, requires a fixed and small set of constants, which is not trivially compressible.

¹The values in this paragraph should *not* be interpreted in terms of clock cycles.

Therefore, the algorithm of BLAKE admits no memory/speed tradeoff; the implementations reported in §3.2, 3.3, and 3.4 thus do not consider memory/speed tradeoffs. The tradeoffs made in the hardware implementations (§3.2) are rather space/speed than memory/speed.

3.1.3 Parallelism

When hashing a message, most of the time spent by the computing unit will be devoted to computing rounds of the compression function. Each round is composed of eight calls to the G function: G_0, G_1, \ldots, G_7 . Simplifying:

- on a serial machine, the speed of a round is about eight times the speed of a G
- on a *parallel* machine, G_0 , G_1 , G_2 and G_3 can be computed in four parallel branches, and then G_4 , G_5 , G_6 and G_7 can be computed in four branches again. The speed of a round is thus about twice the speed of a G

Since parallelism is generally a trade-off, the gain in speed may increase the consumption of other resources (area, etc.). An example of trade-off is to split a round into two branches, resulting in a speed of four times that of a G.

3.2 ASIC and FPGA

We propose four hardware architectures of the BLAKE compression function and report the performances of the corresponding ASIC and FPGA implementations. Similar architectures have been considered by Henzen et al. for VLSI implementations of ChaCha, in [26].

3.2.1 Architectures

The HAIFA iteration mode forces a straightforward hardware implementation of the BLAKE compression function based on a single round unit and a memory to store the internal state variables $\nu_0, \nu_1, \ldots, \nu_{15}$. No pipeline circuits have been designed, due to the enormous resource requirements of such solutions. Nonetheless, several architectures of the compression function have been investigated to evaluate the relation between speed and area. Every implemented circuit reports to the basic block diagram of Fig 3.1.

Besides memory, the four main block components of BLAKE are

- the *initialization* and *finalization* blocks, which are pure combinational logic; initialization contains eight 32/64-bit XOR logic gates to compute the initial state ν, while finalization consists of 24 XOR gates to generate the next chain value.
- the *round function*, which is essentially one or more G functions; G is composed of six modulo $2^{32}/2^{64}$ adders and six XOR gates. Rotations are implemented as a straight rerouting of the internal word bits without any additional logic and without affecting the propagation delay of the circuit.
- the *control unit*, which controls the computation of the compression function, aided by IO enable signals.

Four architectures with different round units have been investigated:

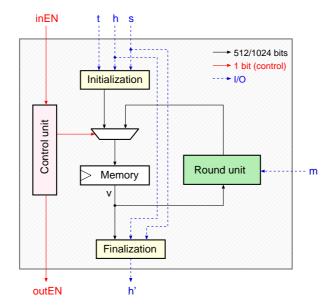


Figure 3.1: Block diagram of the BLAKE compression function. The signals inEn and outEN define the input and output enables.

- [8G]-BLAKE: This design corresponds to the isomorphic implementation of the round function. Eight G function units are instantiated; the first four units work in parallel to compute the column step, while the last four compute the diagonal step.
- [4G]-BLAKE: The round module consists of four parallel G units, which, at a given cycle, compute either the column step or the diagonal step.
- [1G]-BLAKE: The iterative decomposition of the compression function leads to the implementation of a single G function. Thus, one G unit processes the full round in eight cycles.
- $[\frac{1}{2}G]$ -BLAKE: This lightweight implementation consists of a single half G unit. During one cycle, only a single update of the inputs a, b, c, d is processed (i.e., half a G).

In the last three architectures, additional multiplexers and demultiplexers driven by the control unit preserve the functionality of the algorithm, selecting the correct ν elements inside and outside the round unit.

3.2.2 Implementation results

Based on functional VHDL coding (see Appendix B.1), the four designs have been synthesized using a 0.18 µm CMOS technology with the aid of the Synopsys Design Compiler Tool. Table 3.1 summarizes the final values of area, frequency, and throughput². In addition, the hardware efficiency computes the ratio between speed and area of the circuits. The [8G]

 $^{^{2}}$ The unit Gbps means Gigabits per second, where a Gigabit is 1000^{3} bits, not 1024^{3} . Similar rule applies to Mbps and Kbps in Tables 3.1 and 3.2.

and [4G]-BLAKE architectures maximize the throughput, so they were synthesized with speed optimization options at the maximal clock frequency. The target applications of [1G] and $[\frac{1}{2}G]$ -BLAKE are resource-restricted environments, where a compact chip size is the main constraint. Hence, these designs have been synthesized at low frequencies to achieve minimum-area requirements.

Arch.	Function	Area [kGE]	Freq. [MHz]	Latency [cycles]	Throughput [Mbps]	Efficiency [Kbps/GE]
[8G]	BLAKE-32	58.30	114	11	5295	90.8
	BLAKE-64	132.47	87	15	5910	44.6
[4G]	BLAKE-32	41.31	170	21	4153	100.5
	BLAKE-64	82.73	136	29	4810	58.1
[1G]	BLAKE-32	10.54	40	81	253	24.0
	BLAKE-64	20.61	20	113	181	8.8
[¹ / ₂ G]	BLAKE-32	9.89	40	161	127	12.9
	BLAKE-64	19.46	20	225	91	4.7

Table 3.1: ASIC synthesis results. One gate equivalent (GE) corresponds to the area of a two-input drive-one NAND gate of size 9.7 µm².

Three architectures have been implemented on FPGA silicon devices: the Xilinx Virtex-5, Virtex-4, and Virtex-II Pro³. We used SynplifyPro and Xilinx ISE for synthesis and place & route. Table 3.2 reports resulting circuit performances.

	XC2VP50			X	C4VLX10	00	XC5VLX110		
Function	Area	Freq.	Thr.	Area	Freq.	Thr.	Area	Freq.	Thr.
	[slices]	[MHz]	[Mbps]	[slices]	[MHz]	[Mbps]	[slices]	[MHz]	[Mbps]
			[8G]-I	BLAKE aı	chitectu	re			
BLAKE-32	3091	37	1724	3087	48	2235	1694	67	3103
BLAKE-64	11122	17	1177	11483	25	1707	4329	35	2389
			[4G]-I	BLAKE aı	chitectu	re			
BLAKE-32	2805	53	1292	2754	70	1705	1217	100	2438
BLAKE-64	6812	31	1104	6054	40	1413	2389	50	1766
[1G]-BLAKE architecture									
BLAKE-32	958	59	371	960	68	430	390	91	575
BLAKE-64	1802	36	326	1856	42	381	939	59	533

Table 3.2: FPGA post place & route results [overall effort level: standard]. A single Virtex-5 slice contains twice the number of LUTs and FFs.

For the ASIC and the FPGA implementations, the memory of the internal state consists of 16 32/64-bit registers, which are updated every round with the output words of the round unit. No RAM or ROM macro cells are used to store the 16 constants c_0, \ldots, c_{15} . In the same

³Data sheets available at http://www.xilinx.com/support/documentation/

way, the ten permutations $\sigma_0, \ldots, \sigma_9$ have been hard-coded in VHDL. In ASIC, this choice has been motivated by the insufficient memory requirement of these variables. In FPGA, constants and permutations can be stored in dedicated block RAMs. This solution decreases slightly the number of slices needed, but does not speed-up the circuits.

A complete implementation of BLAKE (to include memory storing intermediate values, counter, and circuits to finalize the message, etc.) leads to an increase of about 1.8 kGE or 197 slices for ASIC and FPGA, respectively.

Minimizing the area

An ASIC architecture even smaller than $[\frac{1}{2}G]$ can be reached, by making a circuit only for a quarter (rather than a half) of the G function, and serializing the finalization block. Latency and throughput deteriorate much, but we can reach an area of 8.4 kGE. We omit an extensive description of this architecture because the area reduction from $[\frac{1}{2}G]$ is not worth its cost, in general.

3.2.3 Evaluation

The scalable structure of the round function allows the implementation of distinct architectures, where the trade-off between area and speed differs. Fast circuits are able to achieve throughput about 6 Gbps in ASIC and 3 Gbps in modern FPGA chips, while lightweight architectures require less than 10 kGE or 1000 Slices. BLAKE turns out to be an extremely flexible function, that can be integrated in a wide range of applications, from modern high-speed communication security protocols to low-area RFID systems.

3.3 8-bit microcontroller

The compression function of BLAKE-32 was implemented in a PIC18F2525 microcontroller. About 1800 assembly lines were written, using Microchip's MPLAB Integrated Development Environment v7.6. This section reports results of this implementation, starting with a presentation of the device used. Sample assembly code computing the round function is given in Appendix B.2.

3.3.1 The PIC18F2525

The PIC18F2525 is a member of the PIC family of microcontrollers made by Microchip Technology. PIC's are very popular for embedded systems (more than 6 billions sold). The PIC18F2525 works with 8-bit words, but has an instruction width of 16 bits; it makes up to 10 millions of instructions per second (MIPS).

Following the Harvard architecture, the PIC18F2525 separates program memory and data memory:

- program memory is where the program resides, and can store 48 Kb in flash memory (that is, 24576 instructions)
- data memory is reserved to the data used by the program. It can store 3986 bytes in RAM and 1024 bytes in EEPROM.

Program memory will contain the code of our BLAKE implementation, including the permutations' look-up tables, while variables will be stored in the data memory.

Our PIC processor runs at up to 40 MHz, and a single-cycle instruction takes four clock cycles (10 MIPS). In the following we give cost estimates in terms of instruction cycles, not clock cycles.

Operating frequency	DC – 40 MHz
Program memory (bytes)	49152
Program memory (instructions)	24576
Data memory (bytes)	3968
Data EEPROM (bytes)	1024
Interrupt sources	19
I/O ports	Ports A, B, C, (E)
Timers	4
Serial communication	MSSP, enhanced USART
Parallel communications	no
Instruction set	75 instructions (83 with extended IS)

Table 3.3: Main features of the PIC18F2525

Features of the PIC18F2525 are summarized in Table 3.3. All details can be found on Wikpedia⁴ and in Microchip's datasheet⁵.

3.3.2 Memory management

Our implementation requires 2470 bytes of program memory (including the look-up tables for the permutations), out of 48 Kb available. Data memory stores 274 bytes in RAM for the input variables, constants, and temporary variables, that is:

- message block m (64 bytes)
- chain value h (32 bytes)
- salt s (16 bytes)
- counter t (8 bytes)
- constants c_0, \ldots, c_{15} (64 bytes)
- internal state ν (64 bytes)
- temporary variables (a, b, c, d) for G (16 bytes)
- other temporary variables (10 bytes)

To summarize, BLAKE-32 uses 5% of the program memory, 7% of the RAM, and no EEPROM.

⁴http://en.wikipedia.org/wiki/PIC_micro

⁵http://ww1.microchip.com/downloads/en/DeviceDoc/39626b.pdf

3.3.3 **Speed**

BLAKE-32 only uses the three operations XOR, 32-bit integer addition, and 32-bit rotation. In the PIC18F2525 the basic unit is a byte, not a 32-bit word, hence 32-bit operations have to be simulated with 8-bit instructions:

- 32-bit XOR is simulated by four independent 8-bit XOR's
- 32-bit addition is simulated by four 8-bit additions with manual transfer of the carry between each addition
- 32-bit rotation is simulated using byte swaps and 1-bit rotate instructions

Rotations are the most complicated operations to implement, because a different code has to be written for each rotation distance; rotation of 8 or 16 positions requires no rotate instruction, while one is needed for 7-bit rotation, and four for 12-bit rotation. For example, the code for a 8-bit rotation of $x=x_hi\|x_mh\|x_nl\|x_lo$ looks like

```
movFF x_hi,tmp
movFF x_mh,x_hi
movFF x_ml,x_mh
movFF x_lo,x_ml
movFF tmp,x_lo
```

while the code for a 7-bit rotation looks like

```
bcf STATUS, C
btfsc x_lo,0
bsf STATUS, C
rrcF x_hi
rrcF x_mh
rrcF x_ml
rrcF x_lo
movFF x_lo,tmp
movFF x_hi,x_lo
movFF x_mh,x_hi
movFF x_ml,x_mh
movFF tmp,x_ml
```

In terms of cycles, counting all the instructions needed (rotate, move, etc.), we have that

- >>> 16 needs 6 cycles
- >>> 12 needs 22 cycles
- >>> 8 needs 5 cycles
- >>> 7 needs 12 cycles

Below we detail the maximum cost of each line of the G_i function:

```
 \begin{array}{llll} \mbox{(76 cycles)} & \alpha & \leftarrow & \alpha+b+(m_{\sigma_r(2i)}\oplus c_{\sigma_r(2i+1)}) \\ \mbox{(24 cycles)} & d & \leftarrow & (d\oplus\alpha) \ggg 16 \\ \mbox{(24 cycles)} & c & \leftarrow & c+d \\ \mbox{(34 cycles)} & b & \leftarrow & (b\oplus c) \ggg 12 \\ \mbox{(67 cycles)} & \alpha & \leftarrow & \alpha+b+(m_{\sigma_r(2i+1)}\oplus c_{\sigma_r(2i)}) \\ \mbox{(22 cycles)} & d & \leftarrow & (d\oplus\alpha) \ggg 8 \\ \mbox{(24 cycles)} & c & \leftarrow & c+d \\ \mbox{(29 cycles)} & b & \leftarrow & (b\oplus c) \ggg 7 \\ \end{array}
```

The cycle count is different for $(b \oplus c) \gg 12$ and $(b \oplus c) \gg 7$ because of the different rotation distances. The fifth line needs fewer cycles than the first because of the proximity of the indices (though not of the addresses).

In addition, preparing G_i 's inputs costs 18 cycles, and calling it 4 cycles, thus in total 322 cycles are needed for computing a G_i . Counting the initialization of ν (at most 161 cycles) and the overhead of 8 cycles per round, the compression function needs 26001 cycles (that is, 406 cycles per byte). With a 32 MHz processor (8 MIPS), it takes about 3.250 ms to hash a single message block (a single instruction is 125 ns long); with a 40 MHz processor (10 MIPS), it takes about 2.6 ms.

No precomputation is required to set up the algorithm (BLAKE does not require building internal tables before hashing a message, neither it requires the initialization of a particular data structure, for example). On the PIC18F2525, the only setup cost is for preparing the device, i.e. loading data into the data memory; this cost cannot be expressed (solely) in terms of clock cycles, because of interrupt routines and waiting time, which depend on the data source considered.

For sufficiently large messages (say, a few blocks), the cost of preparing the device and of padding the message is negligible, compared to the cost of computing the compression functions. In this case, generating one message digest with BLAKE-28 or BLAKE-32 on a PIC18F2525 requires about 406 cycles per byte.

3.4 Large processors

BLAKE is easily implemented on 32- and 64-bit processors: it works on words of 32 or 64 bits, and only makes wordwise operations (XOR, rotation, addition) that are implemented in most of the processors. It is based on ChaCha, one of the fastest stream ciphers. The speed-critical code portion is short and thus is relatively easy to optimize. Because the core of BLAKE is just the G function (16 operations), implementations are simple and compact.

As requested by NIST, we wrote a reference implementation and optimized implementations in ANSI C. Here we report speed benchmarks based on the optimized implementation, which will be used by NIST for comparing BLAKE with other candidates. On specific processors, faster implementations can be obtained by programming BLAKE in assembly; one may directly reuse the assembly programs of ChaCha available⁶.

We compiled our program with gcc 4.1.0 with options -03 -fomit-frame-pointer -Wall -ansi. We report speeds for various lengths of (aligned) messages, and give the median measurement over a hundred trials. We measured the time of a call to the function Hash specified in NIST's API, which includes

⁶See http://cr.yp.to/chacha.html

- 1. function Init: initialization of the function parameters, copy of the instance's IV
- 2. function Update: iterated hash of the message
- 3. function Final: padding of the message, compression (at most two) of the remaining data

Table 3.4 reports the number of clock cycles required to generate one message digest with the full versions of BLAKE-32 and BLAKE-64 and for reduced-round versions, depending on the message length. BLAKE-28 and BLAKE-48 show performance similar to BLAKE-32 and BLAKE-64, respectively. The "Core 2 Duo" platform corresponds to the *NIST SHA-3 Reference Platform*, except that our computer was running Linux instead of Windows Vista.

For any digest length, a negligible number of cycles is required to setup the algorithm. This is because no precomputation is necessary, and the only preparation consists in loading data in memory.

Data length [bytes]	10	100	1000	10000			
Celeron M (32-bit mode)							
BLAKE-32 (10 rounds)	≈1500	50.1	24.5	22.2			
BLAKE-32 (8 rounds)	\approx 1500	56.5	21.7	18.5			
BLAKE-32 (5 rounds)	≈1500	43.2	13.9	12.5			
BLAKE-64 (14 rounds)	≈2000	126.4	64.4	58.8			
BLAKE-64 (10 rounds)	\approx 2000	99.7	47.7	43.1			
BLAKE-64 (7 rounds)	≈2000	93.5	32.5	30.8			
Core 2 D	uo (32-bi	t mode)					
BLAKE-32 (10 rounds)	≈2900	51.5	27.4	28.3			
BLAKE-32 (8 rounds)	\approx 2900	45.2	22.6	24.2			
BLAKE-32 (5 rounds)	≈2900	35.0	15.9	14.0			
BLAKE-64 (14 rounds)	≈4400	94.0	61.3	61.7			
BLAKE-64 (10 rounds)	\approx 4400	74.0	45.4	57.6			
BLAKE-64 (7 rounds)	≈4400	58.9	32.5	41.0			
Core 2 D	uo (64-bi	t mode)					
BLAKE-32 (10 rounds)	≈1600	36.4	18.4	16.7			
BLAKE-32 (8 rounds)	\approx 1600	32.2	15.4	13.8			
BLAKE-32 (5 rounds)	≈1600	26.9	10.9	9.6			
BLAKE-64 (14 rounds)	≈1900	33.7	13.8	12.3			
BLAKE-64 (10 rounds)	\approx 1900	29.9	11.6	9.3			
BLAKE-64 (7 rounds)	≈1900	26.8	8.5	7.2			

Table 3.4: Performance of our optimized C implementation of BLAKE (in cycles/byte), on a 900 MHz Intel Celeron M and a 2.4 GHz Intel Core 2 Duo.

In terms of bytes-per-second, the top speed is achieved by BLAKE-64 in 64-bit mode, with about 317 Mbps. For very small messages (10 bytes) the overhead is due to the compression of 64 (respectively 128) bytes, and to the cost of initializing and padding the message. The cost per byte quickly decreases, and stabilizes after 1000-byte messages. Although different

processors were used, our estimates can be compared with the fastest C implementation of SHA-256, by Gladman⁷: in 64-bit mode on a AMD processor, SHA-256 runs at 20.4 cyclesper-byte, and SHA-512 at 13.4 cycles-per-byte.

 $^{^{7} \}texttt{http://fp.gladman.plus.com/cryptography_technology/sha/index.htm}$

4 Using BLAKE

BLAKE is intended to replace SHA-2 with a minimal engineering effort, and to be used wherever SHA-2 is. BLAKE provides the same interface as SHA-2, with the optional input of a salt. BLAKE is suitable whenever a cryptographic hash function is needed, be it for digital signatures, MAC's, commitment, password storage, key derivation, etc.

This chapter explains how the salt input should (not) be used, and construction details based on BLAKE for HMAC and UMAC, PRF ensembles, and randomized hashing.

4.1 Hashing with a salt

The BLAKE hash functions take as input a message and a salt. The aim of hashing with distinct salts is to hash with different functions but using the same algorithm. Depending on the application, the salt can be chosen randomly (thus reusing a same salt twice can occur, though with small probability), or derived from a counter (nonce).

For applications in which no salt is required, it is set to the null value (s=0). In this case the initialization of the state ν simplifies to

$$\begin{pmatrix} v_0 & v_1 & v_2 & v_3 \\ v_4 & v_5 & v_6 & v_7 \\ v_8 & v_9 & v_{10} & v_{11} \\ v_{12} & v_{13} & v_{14} & v_{15} \end{pmatrix} \leftarrow \begin{pmatrix} h_0 & h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 & h_7 \\ c_0 & c_1 & c_2 & c_3 \\ t_0 \oplus c_4 & t_0 \oplus c_5 & t_1 \oplus c_6 & t_1 \oplus c_7 \end{pmatrix}$$

and the finalization of the compression function becomes

The salt input may contain a nonce or a random seed, for example. A typical application is for password storage. However, the salt input is not intended to contain the secret key for a MAC construction. We recommend using HMAC or UMAC for MAC functionality, which are much more efficient.

4.2 HMAC and UMAC

HMAC [6] can be built on BLAKE similarly to SHA-2. The salt input is not required, and should thus be set to zero (see 4.1). BLAKE has no property that limits its use for HMAC, compared to SHA-2. For example, HMAC based on BLAKE-32 takes as input a key k and a message m and computes

$$\mathsf{HMAC}_k(\mathfrak{m}) = \mathsf{BLAKE-32}(k \oplus \mathsf{opad} || \mathsf{BLAKE-32}(k \oplus \mathsf{ipad} || \mathfrak{m})).$$

All details on the HMAC construction are given in the NIST standardization report [35] or in the original publication [6].

UMAC is a MAC construction "faster but more complex" [13] than HMAC: it is based on the "PRF(hash, nonce)" approach, where the value "hash" is a universal hash of the message authenticated. UMAC authors propose to instanciate the PRF with HMAC based on SHA-1, computing HMAC $_k$ (nonce||hash).

For combining BLAKE with UMAC, the same approach can be used, namely using HMAC based on BLAKE. It is however more efficient to use BLAKE's salt, and thus compute HMAC(hash) with $s=\mathsf{nonce}$:

$$\mathsf{HMAC}_k(\mathsf{hash}) = \mathsf{BLAKE-32}(k \oplus \mathsf{opad} \| \mathsf{BLAKE-32}(k \oplus \mathsf{ipad} \| \mathsf{hash}, \mathsf{nonce}), \mathsf{nonce})$$

In the best case, setting s = nonce saves one compression compared to the original construction, while in the worst case performance is unchanged. UMAC authors suggest a nonce of 64 bits [13], which fits in the salt input of all BLAKE functions. We recommend this construction for UMAC based on BLAKE.

4.3 PRF ensembles

To construct pseudorandom functions (PRF) ensembles from hash functions, a common practice is to append or prepend the index data to the message. For example, for an arbitrary message \mathfrak{m} one can define the \mathfrak{i}^{th} function of the ensemble as

BLAKE-32(
$$m|i$$
) or BLAKE-32($i|m$)

where i is encoded over a fixed number of bits. These techniques pose no problem specific to BLAKE. The second construction is even more secure than with SHA-2, because it makes some length-extension attacks impossible (cf. $[6, \S 6]$ and $\S 5.5.1$).

Another technique proposed for constructing PRF ensembles is to modify the IV according to the index data. That is, the \mathfrak{i}^{th} function of the ensemble has an IV equal to (some representation of) \mathfrak{i} . A concrete construction that exploits this technique is NMAC [6], which computes a MAC as

$$\mathsf{NMAC}_{k_1 \parallel k_2}(\mathfrak{m}) = \mathsf{H}_{k_1} \big(\mathsf{H}_{k_2}(\mathfrak{m}) \big)$$

where H_k is a hash function with initial value k.

For combining BLAKE with NMAC, we recommend not to set directly IV \leftarrow k_i , i=1,2, but instead IV \leftarrow **compress**(IV, i, 0, 0), starting from the IV specific to the function used. This makes the effective IV dependent on the function instance (cf. §2.1 and §2.3).

A last choice for constructing PRF's based on BLAKE is to use the salt for the index data, giving ensembles of 2^{128} and 2^{256} for BLAKE-32 and BLAKE-64, respectively.

4.4 Randomized hashing

Randomized hashing is mainly used for digital signatures (cf. [24,37]): instead of sending the signature Sign(H(m)), the signer picks a random r and sends $(Sign(H_r(m)), r)$ to the verifier. The advantage of randomized hashing is that it relaxes the security requirements of the hash function [24]. In practice, random data is either appended/prepended to the message or combined with the message; for example the RMX transform [24], given a random r, hashes m to the value

$$H(r\|(m^1\oplus r)\|\dots\|(m^{N-1}\oplus r)).$$

BLAKE offers a dedicated interface for randomized hashing, not a modification of a non-randomized mode: the input s, 128 or 256 bits long, should be dedicated for the salt of randomized hashing. This avoids the potential computation overhead of other methods, and allows the use of the function as a blackbox, rather than a special mode of operation of a classical hash function. BLAKE remains compatible with previous generic constructions, including RMX.

5 Elements of analysis

This chapter presents a preliminary analysis of BLAKE, with a focus on BLAKE-32. We study properties of the function's components, resistance to generic attacks, and dedicated attack strategies.

5.1 Permutations

The permutations σ_0,\ldots,σ_9 were chosen to match several security criteria: First we ensure that a same input difference doesn't appear twice at the same place (to complicate "correction" of differences in the state). Second, for a random message all values $(\mathfrak{m}_{\sigma_r(2i)}\oplus c_{\sigma_r(2i+1)})$ and $(\mathfrak{m}_{\sigma_r(2i+1)}\oplus c_{\sigma_r(2i)})$ should be distinct with high probability. For chosen messages, this guarantees that each message word will be XOR'd with different constants, and thus apply distinct transformations to the state through rounds. It also implies that no pair $(\mathfrak{m}_i,\mathfrak{m}_j)$ is input twice in the same G_i . Finally, the position of the inputs should be balanced: in a round, a given message word is input either in a column step or in a diagonal step, and appears either first or second in the computation of G_i . We ensure that each message word appears as many times in a column step as in a diagonal step, and as many times first as second within a step. To summarize:

- 1. no message word should be input twice at the same point
- 2. no message word should be XOR'd twice with the same constant
- 3. each message word should appear exactly 5 times in a column step and 5 times in a diagonal step
- 4. each message word should appear exactly 5 times in first position in G and 5 times in second position

This is equivalent to say that, in the representation of permutations in §2.1.1 (also see Table 5.1):

- 1. for all i = 0, ..., 15, there should exist no distinct permutations σ, σ' such that $\sigma(i) = \sigma'(i)$
- 2. no pair (i,j) should appear twice at an offset of the form (2k,2k+1), for all $k=0,\ldots,7$
- 3. for all $i=0,\ldots,15$, there should be 5 distinct permutations σ such that $\sigma(i)<8$, and 5 such that $\sigma(i)>8$
- 4. for all $i=0,\ldots,15$, there should be 5 distinct permutations σ such that $\sigma(i)$ is even, and 5 such that $\sigma(i)$ is odd

In BLAKE-64, four of the permutations are repeated because it makes 14 rounds instead of 10. The above criteria thus just apply to the first ten rounds. The slight loss of balance in the four last rounds seems unlikely to affect security.

Round	G	60	G	3 1	G	2	G	3	G	i 4	G	5	G	6	G	3 7
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	14	10	4	8	9	15	13	6	1	12	0	2	11	7	5	3
2	11	8	12	0	5	2	15	13	10	14	3	6	7	1	9	4
3	7	9	3	1	13	12	11	14	2	6	5	10	4	0	15	8
4	9	0	5	7	2	4	10	15	14	1	11	12	6	8	3	13
5	2	12	6	10	0	11	8	3	4	13	7	5	15	14	1	9
6	12	5	1	15	14	13	4	10	0	7	6	3	9	2	8	11
7	13	11	7	14	12	1	3	9	5	0	15	4	8	6	2	10
8	6	15	14	9	11	3	0	8	12	2	13	7	1	4	10	5
9	10	2	8	4	7	6	1	5	15	11	9	14	3	12	13	0

Table 5.1: Input of message words.

5.2 Compression function

This section reports a bottom-up analysis of BLAKE's compression function.

5.2.1 G function

Given (a, b, c, d) and message block(s) m_j , $j \in \{0, ..., 15\}$; a function G_i computes

$$\begin{array}{lll} \boldsymbol{a} & \leftarrow & \boldsymbol{a} + \boldsymbol{b} + (m_{\sigma_r(2i)} \oplus \boldsymbol{c}_{\sigma_r(2i+1)}) \\ \boldsymbol{d} & \leftarrow & (\boldsymbol{d} \oplus \boldsymbol{a}) \ggg 16 \\ \boldsymbol{c} & \leftarrow & \boldsymbol{c} + \boldsymbol{d} \\ \boldsymbol{b} & \leftarrow & (\boldsymbol{b} \oplus \boldsymbol{c}) \ggg 12 \\ \boldsymbol{a} & \leftarrow & \boldsymbol{a} + \boldsymbol{b} + (m_{\sigma_r(2i+1)} \oplus \boldsymbol{c}_{\sigma_r(2i)}) \\ \boldsymbol{d} & \leftarrow & (\boldsymbol{d} \oplus \boldsymbol{a}) \ggg 8 \\ \boldsymbol{c} & \leftarrow & \boldsymbol{c} + \boldsymbol{d} \\ \boldsymbol{b} & \leftarrow & (\boldsymbol{b} \oplus \boldsymbol{c}) \ggg 7 \end{array}$$

The G function is inspired from the "quarter-round" function of the stream cipher ChaCha, which transforms (a, b, c, d) as follows:

$$\begin{array}{lll} a & \leftarrow & a+b \\ d & \leftarrow & (d\oplus a) \lll 16 \\ c & \leftarrow & c+d \\ b & \leftarrow & (b\oplus c) \lll 12 \\ a & \leftarrow & a+b \\ d & \leftarrow & (d\oplus a) \lll 8 \\ c & \leftarrow & c+d \\ b & \leftarrow & (b\oplus c) \lll 7 \end{array}$$

To build BLAKE's compression function based on this algorithm, we add input of two message words and constants, and let the function be otherwise unchanged. We keep the rotation distances of ChaCha, which provide a good trade-off security/efficiency: 16- and 8-bit rotations

preserve byte alignment, so are fast on 8-bit processors (no rotate instruction is needed), while 12- and 7-bit rotations break up the byte structure, and are reasonably fast.

ChaCha's function is itself an improvement of the "quarter round" of the stream cipher Salsa20. The idea of a 4×4 state with four parallel mappings for rows and columns goes back to the cipher Square [18], and was then successfuly used in Rijndael [19], Salsa20 and ChaCha. Detailed design rationale and preliminary analysis of ChaCha and Salsa20 can be found in [7,9], and cryptanalysis in [3,17,27,39].

Bijectivity

Given a message m, and a round index r, the inverse function of G_i is defined as follows:

$$\begin{array}{lll} b & \leftarrow & c \oplus (b \lll 7) \\ c & \leftarrow & c - d \\ d & \leftarrow & a \oplus (d \lll 8) \\ a & \leftarrow & a - b - (m_{\sigma_r(2i+1)} \oplus c_{\sigma_r(2i)}) \\ b & \leftarrow & c \oplus (b \ggg 12) \\ c & \leftarrow & c - d \\ d & \leftarrow & a \oplus (d \ggg 16) \\ a & \leftarrow & a - b - (m_{\sigma_r(2i)} \oplus c_{\sigma_r(2i+1)}) \end{array}$$

Hence for any (a',b',c',d'), one can efficiently compute the unique (a,b,c,d) such that $G_i(a,b,c,d)=(a',b',c',d')$, given i and m. In other words, G_i is a permutation of $\{0,1\}^{128}$.

Linear approximations

We found several linear approximations of differentials; the notation $(\Delta_0, \Delta_1, \Delta_2, \Delta_3) \mapsto (\Delta_0', \Delta_1', \Delta_2', \Delta_3')$ means that the two inputs with the leftmost difference lead to outputs with the rightmost difference, when $(\mathfrak{m}_{\sigma_r(2i+1)} \oplus c_{\sigma_r(2i)}) = (\mathfrak{m}_{\sigma_r(2i+1)} \oplus c_{\sigma_r(2i+1)}) = 0$. For random inputs we have for example

- (80000000, 00000000, 80000000, 80008000) → (80000000, 0, 0, 0) with probability 1
- $(00000800, 80000800, 80000000, 80000000) \mapsto (0, 0, 80000000, 0)$, with probability 1/2
- $(80000000, 80000000, 80000080, 00800000) \mapsto (0, 0, 0, 80000000)$, with probability 1/2

Many high probability differentials can be identified for G, and one can use standard message modification techniques (linearization, neutral bits) to identify a subset of inputs for which the probability is much higher than for the whole domain. Similar linear differentials exist in the Salsa20 function, and were exploited [3] to attack the compression function Rumba [8], breaking 3 rounds out of 20.

Particular properties of G are

- 1. the only fixed-point in G is the zero input
- 2. no preservation of differences can be obtained by linearization

The first observation is straightforward when writing the corresponding equations. The second point means that there exist no pair of inputs whose difference (according to XOR) is preserved in the corresponding pair of outputs, in the linearized model. This follows from the fact that, if an input difference gives the same difference in the output, then this difference must be a fixed-point for G; since the only fixed-point is the null value, there exists no such difference.

Diffusion

Diffusion is the ability of the function to quickly spread a small change in the input through the whole internal state. For example, G inputs message words such that any difference in a message word affects the four words output. Tables 5.2.1 and 5.3 give the average number of bits modified by G, given a random one-bit difference in the input, for each input word.

in\out	a	b	С	d
а	4.6	11.7	10.0	6.5
b	6.6	11.7 14.0	11.5	8.4
c	2.4	6.6 8.4	4.8	2.4
d	2.4	8.4	6.7	3.4

Table 5.2: Average number of changes in each output word given a random bit flip in each input word.

in\out	a	b	c	d
а	4.4	9.9 12.4	8.2	6.3
b	6.3	12.4	9.8	8.1
c	1.9	3.9	2.9	1.9
d	1.9	4.9	3.9	2.9

Table 5.3: Average number of changes in each output word given a random bit flip in each input word, in the XOR-linearized model.

5.2.2 Round function

The round function of BLAKE is

Bijectivity

Because G is a permutation, a round is a permutation of the inner state ν for any fixed message. In other words, given a message and the value of ν after r rounds, one can determine the value of ν at rounds r-1, r-2, etc., and thus the initial value of ν . Therefore, for a same initial state a sequence of rounds is a permutation of the message. That is, one cannot find two messages that produce the same internal state, after any number of rounds.

Diffusion and low-weight differences

After one round, all 16 words are affected by a modification of one bit in the input (be it the message, the salt, or the chain value). Here we illustrate diffusion through rounds with a concrete example, for the *null message* and the *null initial state*. The matrices displayed below

represent the *differences* in the state after each step of the first two rounds (column step, diagonal step, column step, diagonal step), for a difference in the least significant bit of v_0 :

column step	00000037 E06E0216 37010B00 37000700	00000000 00000000 00000000 00000000	00000000 00000000 00000000 00000000	00000000 00000000 00000000 00000000)	(weight 34)
diagonal step	0000027F 66918CC7 F8D104F0 151703A7	10039015 1CBEEE25 6F08C6F9 705002B0	5002B070 F1A8535F 5F77131E F2C22207	C418A7D4 C111AD29 E4291FE7 7F001702	(weight 219)
column step	944F85FD A729BBE9 7BF5F768 5A1642B3	A044CCB3 6549BC3D 7831614B 41B00EA0	9476A6BC 3A330361 CF44C968 A7115A95	24B6ADAC 7318B20D 53D886E2 7AC791D1	(weight 249)
diagonal step	DFC2D878 FC91AF81 FB98AF71 F042BB72	F9FAAE7A D78E2315 DC27330E 1C7A59AB	2D804D9A 55048021 47A19B59 AC2EFFA4	3EF58B7F 0811CC46 EDDE442E 2E76390B	(weight 264)

In comparison, in the linearized model (i.e., where all additions are replaced by XOR's), we have:

The higher weight in the original model is due to the addition carries induced by the constants c_0, \ldots, c_{15} . A technique to avoid carries at the first round and get a low-weight output difference is to choose a message such that $m_0 = c_0, \ldots, m_{15} = c_{15}$. At the subsequent rounds, however, nonzero words are introduced because of the different permutations.

Diffusion can be delayed a few steps by combining high-probability and low-weight differentials of G, using initial conditions, neutral bits, etc. For example, applying directly the differential

 $(80000000,00000000,80000000,80008000) \mapsto (80000000,0,0,0)$

the diffusion is delayed one step, as illustrated below:

column step	80000000 00000000 00000000	00000000 00000000 00000000	00000000 0000000 0000000 0000000	00000000 00000000 00000000	(weight 1)
diagonal step	800003E8 00000000 00000000 00000000	00000000 0B573F03 00000000 00000000	00000000 00000000 AB9F819D 00000000	00000000 00000000 00000000 E8800083	(weight 49)
column step	8007E4A0 5944FE53 A27F0D24 A08FFF64	2075B261 F178A22F 98D6929A 2AD374B7	18E78828 86B0A65B 4088A5FB 2818E788	9800099E 936C73CB 2E39EDA3 1E9883E1	(weight 236)
diagonal step	4B3CBDD2 3A023C96 9DCA344A FC81FE81	0290847F 49908E86 827BF1E5 D676FFC9	B4FF78F9 F13BC1D7 B20A8825 80740480	F1E71BA3 ADC2020A FE575BE3 52570CB2	(weight 252)

In comparison, for a same input difference in the linearized model we have

These examples show that even in the linearized model, after two rounds about half of the state bits have changed when different initial states are used (similar figures can be given for a difference in the message). Using clever combinations of low-weight differentials and message modifications one may attack reduced versions with two or three rounds. However, differences after more than four steps seem very difficult to control.

5.2.3 Compression function

BLAKE's compression function is the combination of an initialization, a sequence of rounds, and a finalization. Contrary to ChaCha, BLAKE breaks self-similarity by using a round-dependent permutation of the message and the constants. This prevents attacks that exploit the similarity

among round functions (cf. slide attacks in §5.6.3). Particular properties of the compression function are summarized below.

Initialization

At the initialization stage, constants and redundancy of t impose a nonzero initial state (and a non "all-one" state). The disposition of inputs implies that after the first column step the initial value h is directly mixed with the salt s and the counter t.

The double input of t_0 and t_1 in the initial state suggests the notion of *valid* initial state: we shall call an initial state ν_0,\ldots,ν_{15} valid if and only there exists t_0,t_1 such that $\nu_{12}=t_0\oplus c_4$ and $\nu_{13}=t_0\oplus c_5$, and $\nu_{14}=t_1\oplus c_6$ and $\nu_{15}=t_1\oplus c_7$. Non-valid states are thus impossible initial states.

Number of rounds

The choice of 10 rounds for BLAKE-32 was determined by

- 1. the cryptanalytic results on Salsa20, ChaCha, and Rumba (one BLAKE-32 round is essentially two ChaCha rounds, so the initial conservative choice of 20 rounds for ChaCha corresponds to 10 rounds for BLAKE-32): truncated differentials were observed for up to 4 Salsa20 rounds and 3 ChaCha rounds, and the Rumba compression function has shortcut attacks for up to 3 rounds; the eSTREAM project chose a version of Salsa20 with 12 rounds in its portfolio, and 12-round ChaCha is arguably as strong as 12-round Salsa20.
- 2. our results on early versions of BLAKE, which had similar high-level structure, but a round function different from the present one: for the worst version, we could find collisions for up to 5 rounds.
- 3. our results on the final BLAKE: full diffusion is achieved after two rounds, and the best differentials found can be used to attack two rounds only.

BLAKE-64 has 14 rounds, i.e., 4 more than BLAKE-32; this is because the larger state requires more rounds for achieving similar security (in comparison, SHA-512 has 1.25 times more rounds than SHA-256).

We believe that the choice of 10 and 14 rounds provides a high security margin, without sacrificing performance. The number of rounds may later be adjusted according to the future results on BLAKE (for example, 8 rounds for BLAKE-32 may be fine if the best attack breaks 4 rounds, while 12 rounds may be chosen if an attack breaks, say, 6 rounds).

Finalization

At the finalization stage, the state is compressed to half its length, in a way similar to that of the cipher Rabbit [14]. The feedforward of h and s makes each word of the hash value dependent on two words of the inner state, one word of the initial value, and one word of the salt. The goal is to make the function non-invertible when the initial value and/or the salt are unknown.

Our approach of "permutation plus feedforward" is similar to that of SHA-2, and can be seen as a particular case of Davies-Meyer-like constructions: denoting E the blockcipher defined by the round sequence, BLAKE's compression function computes

$$\mathsf{E}_{\mathsf{m}||\mathsf{s}}(\mathsf{h}) \oplus \mathsf{h} \oplus (\mathsf{s}||\mathsf{s})$$

which, for a null salt, gives the Davies-Meyer construction $E_{\mathfrak{m}}(\mathfrak{h}) \oplus \mathfrak{h}$. We use XOR's and not additions (as in SHA-2), because here additions don't increase security, and are much more expensive in circuits and 8-bit processors.

If the salt *s* was unknown and not fedforward, then one would be able to recover it given a one-block message, its hash value, and the IV. This would be a critical property. The counter t is not input in the finalization, because its value is always known and never chosen by the users.

Local collisions

A *local collision* happens when, for two distinct messages, the internal states after a same number of rounds are identical. For BLAKE hash functions, there exists no local collisions for a same initial state (i.e., same IV, salt, and counter). This result directly follows from the fact that the round function is a permutation of the message, for fixed initial state ν (and so different inputs lead to different outputs). This property generalizes to any number of rounds. The requirement of a same initial state does not limit much the result: for most of the applications, no salt is used, and a collision on the hash function implies a collision on the compression function with same initial state [10].

Full diffusion

Full diffusion is achieved when each input bit has a chance to affect each output bit. BLAKE-32 and BLAKE-64 achieve full diffusion after two rounds, given a difference in the IV, m, or s.

5.2.4 Fixed-points

A fixed-point for BLAKE's compression function is a tuple (m, h, s, t) such that

$$compress(m, h, s, t) = h$$

Functions of the form $E_m(h) \oplus h$ (like SHA-2) allow the finding of fixed-points for chosen messages by computing $h = E^{-1}(0)$, which gives $E_m(h) \oplus h = h$.

BLAKE's structure is a particular case of the Davies-Meyer-like constructions mentioned in §5.2.3; consider the case when no salt is used (s = 0), without loss of generality; for finding fixed-points, we have to choose the final ν such that

 $\begin{array}{lll} h_0 & = & h_0 \oplus \nu_0 \oplus \nu_8 \\ h_1 & = & h_1 \oplus \nu_1 \oplus \nu_9 \\ h_2 & = & h_2 \oplus \nu_2 \oplus \nu_{10} \\ h_3 & = & h_3 \oplus \nu_3 \oplus \nu_{11} \\ h_4 & = & h_4 \oplus \nu_4 \oplus \nu_{12} \\ h_5 & = & h_5 \oplus \nu_5 \oplus \nu_{13} \\ h_6 & = & h_6 \oplus \nu_6 \oplus \nu_{14} \\ h_7 & = & h_7 \oplus \nu_7 \oplus \nu_{15} \end{array}$

That is, we need $v_0 = v_8, v_1 = v_9, \dots, v_7 = v_{15}$, so there are 2^{256} possible choices for v. From this v we compute the round function backward to get the initial state, and we find a fixed-point when

- the third line of the state is c_0, \ldots, c_3 , and
- the fourth line of the state is valid, that is, $v_{12} = v_{13} \oplus c_4 \oplus c_5$ and $v_{14} = v_{15} \oplus c_6 \oplus c_7$

Thus we find a fixed-point with effort $2^{128} \times 2^{64} = 2^{192}$, instead of 2^{256} ideally. This technique also allows to find several fixed-points for a same message (up to 2^{64} per message) in less time than expected for an ideal function.

BLAKE's fixed-point properties do not give a distinguisher between BLAKE and a PRF, because we use here the internal mechanisms of the compression function, and not blackbox queries.

Fixed-point collisions

A fixed-point collision for BLAKE is a tuple (m, m', h, s, s', t, t') such that

$$compress(m, h, s, t) = compress(m', h, s', t') = h,$$

that is, a pair of fixed-points for the same hash value. This notion was introduced in [2], which shows that fixed-point collisions can be used to build multicollisions at a reduced cost. For BLAKE-32, however, a fixed-point collision costs about $2^{192} \times 2^{128} = 2^{320}$ trials, which is too high to exploit for an attack.

5.3 Iteration mode (HAIFA)

HAIFA [10, 23] is a general iteration mode for hash functions, which can be seen as "Merkle-Damgård with a salt and a counter". HAIFA offers an interface for input of the salt and the counter, and provides resistance to several generic attacks (herding, long-message second preimages, length extension). HAIFA was used for the LAKE hash functions [5], and analyzed in [1, 15].

Below we comment on BLAKE's use of HAIFA:

- HAIFA has originally a single IV for a family of functions, and computes the effective IV of a specific instance with k-bit hashes by setting IV ← compress(IV, k, 0, 0). This allows variable-length hashing, but complicates the function and requires an additional compression. BLAKE has only two different instances for each function, so we directly specify their proper IV to simplify the definition. Each instance has a distinct effective IV, but no extra compression is needed.
- HAIFA defines a padding data that includes the encoding of the hash value length; again, because we only have two different lengths, one bit suffices to encode the identity of the instance (i.e., 1 encodes 256, and 0 encodes 224). We preserve the instance-dependent padding, but reduce the data overhead, and in the best case save one call to the compression function. Padding the binary encoding of the hash bit length wouldn't increase security.

On the role of the counter

We will highlight some facts that underlie HAIFA's resistance to length extension and second preimage attacks. Suppose that $\mathbf{compress}(\cdot, \cdot, \cdot, t)$ defines a family of pseudorandom functions (PRF's); to make clear the abstraction we'll write $\{F_t\}_t$ the PRF family, such that

 $F_t(m,h,s)=h'$, i.e. F is an ideal compression function, and F_t an ideal compression function with counter set to t. In the process of iteratively hashing a message, all compression functions F_t are different, because the counter is different at each compression. For example, when hashing a 1020-bit message with BLAKE-32, we first use F_{512} , then F_{1020} , and finally F_0 .

Now observe that the family $\{F_t\}$ can be split into two disjoint sets (considering BLAKE-32's parameters):

 the intermediate compressions, called to compress message blocks containing no padding data (only original message bits):

$$\mathcal{I} = \{ \mathbf{F_t}, \exists k \in \mathbb{N}^*, t = 512 \cdot k \le 2^{64} - 512 \}$$

2. the final compressions, called to compress message blocks containing padding data:

$$\mathcal{F} = \{F_0\} \cup \{F_t, \exists k \in \mathbb{N}^*, p \in \{1, \dots, 511\}, t = 512 \cdot k + p < 2^{64}\}$$

A function in $\mathcal I$ is never the last in a chain of iterations. A function in $\mathcal F$ appears either in last or penultimate position, and its inputs are restricted to message blocks with consistent padding (for example F_{10} in BLAKE-32 needs messages of the form $\langle 10 \text{ bits} \rangle 10 \dots 01 \langle 10 \rangle_{64}$). Clearly, $|\mathcal I| = 2^{55} - 1$ and $|\mathcal F| = 511 \cdot |\mathcal I|$. Functions in $\mathcal F$ can be seen as playing a role of output filter, in the same spirit as the NMAC hash construction [16].

The above structure is behind the original security properties of HAIFA, including its resistance to second-preimage attacks [23].

5.4 Pseudorandomness

One expects from a good hash function to "look like a random function". Notions of indistinguishability, unpredictability, indifferentiability [31] and seed-incompressibility [25] define precise notions related to "randomness" for hash functions, and are used to evaluate generic constructions or dedicated designs. However they give no clue on how to construct primitives' algorithms.

Roughly speaking, the algorithm of the compression function should simulate a "complicated function", with no apparent structure—i.e., it should have no property that a random function has not. In terms of structure, "complicated" means for example that the algebraic normal form (ANF) of the function, as a vector of Boolean functions, should contain each possible monomial with probability 1/2; generalizing, it means that when any part of the input is random, then the ANF obtained by fixing this input is also (uniform) random. Put differently, the truth table of the hash function when part of the input is random should "look like" a random bit string. In terms of input/output, "complicated" means for example that a small difference in the input doesn't imply a small difference in the input; more generally, any difference or relation between two inputs should be statistically independent of any relation of the corresponding outputs.

Pseudorandomness is particularly critical for stream ciphers, and no distinguishing attack—or any other non-randomness property—has been identified on Salsa20 or ChaCha. These ciphers construct a complicated function by making a long chain of simple operations. Non-randomness was observed for reduced versions with up to three ChaCha rounds (which correspond to one and a half BLAKE round). BLAKE inherits ChaCha's pseudorandomness, and in addition avoids the self-similarity of the function by having round-dependent constants. Although there is no formal reduction of BLAKE's security to ChaCha's, we can reasonably conjecture that BLAKE's compression function is "complicated enough" with respect to pseudorandomness.

5.5 Generic attacks

This section reports on the resistance of BLAKE to the most important generic attacks, that is, attacks that exploit to broad class of functions: for example a generic attack can exploit the iteration mode, or weak algebraic properties of the compression function.

5.5.1 Length extension

Length extension is a forgery attack against MAC's of the form $H_k(\mathfrak{m})$ or $H(k\|\mathfrak{m})$, i.e. where the key k is respectively used as the IV or prepended to the message. The attack can be applied when H is an iterated hash with "MD-strengthening" padding: given $h = H_k(\mathfrak{m})$ and \mathfrak{m} , determine the padding data \mathfrak{p} , and compute $\mathfrak{v}' = H_k(\mathfrak{m}')$, for an arbitrary \mathfrak{m}' . It follows from the iterated construction that $\mathfrak{v}' = H_k(\mathfrak{m}\|\mathfrak{p}\|\mathfrak{m}')$. That is, the adversary forged a MAC of the message $\mathfrak{m}\|\mathfrak{p}\|\mathfrak{m}'$.

The length extension attack doesn't apply to BLAKE, because of the input of the number of bits hashed so far to the compression function, which simulates a specific output function for the last message block (cf. §5.3). For example, let \mathfrak{m} be a 1020-bit message; after padding, the message is composed of three blocks $\mathfrak{m}^0, \mathfrak{m}^1, \mathfrak{m}^2$; the final chain value will be $\mathfrak{h}^3 = \text{compress}(\mathfrak{h}^2, \mathfrak{m}^2, s, 0)$, because counter values are respectively 512, 1020, and 0 (see §2.1.3). If we extend the message with a block \mathfrak{m}^3 , with convenient padding bits, and hash $\mathfrak{m}^0 \| \mathfrak{m}^1 \| \mathfrak{m}^2 \| \mathfrak{m}^3$, then the chain value between \mathfrak{m}^2 and \mathfrak{m}^3 will be $\text{compress}(\mathfrak{h}^2, \mathfrak{m}^2, s, 1024)$, and thus be different from $\text{compress}(\mathfrak{h}^2, \mathfrak{m}^2, s, 0)$. The knowledge of BLAKE-32($\mathfrak{m}^0 \| \mathfrak{m}^1 \| \mathfrak{m}^2$) cannot be used to compute the hash of $\mathfrak{m}^0 \| \mathfrak{m}^1 \| \mathfrak{m}^2 \| \mathfrak{m}^3$.

5.5.2 Collision multiplication

We coin the term "collision multiplication" to define the ability, given a collision $(\mathfrak{m},\mathfrak{m}')$, to derive an arbitrary number of other collisions. For example, Merkle-Damgård hash functions allow to derive collisions of the form $(\mathfrak{m}\|\mathfrak{p}\|\mathfrak{u},\mathfrak{m}'\|\mathfrak{p}'\|\mathfrak{u})$, where \mathfrak{p} and \mathfrak{p}' are the padding data, and \mathfrak{u} an arbitrary string; this technique can be seen as a kind of length extension attack. And for the same reasons that BLAKE resists length extension, it also resists this type of collision multiplication, when given a collision of minimal size (that is, when the collision only occurs for the hash value, not for intermediate chain values).

5.5.3 Multicollisions

A multicollision is a set of messages that map to the same hash value. We speak of a k-collision when k distinct colliding messages are known.

Joux's technique

The technique proposed by Joux [28] finds a k-collision for Merkle-Damgård hash functions with n-bit hash values in $\lceil \log_2 k \rceil \cdot 2^{n/2}$ calls to the compression function (see Fig. 5.1). The colliding messages are long of $\lceil \log_2 k \rceil$ blocks. This technique applies as well for the BLAKE hash functions, and to all hash functions based on HAIFA. For example, a 32-collision for BLAKE-32 can be found within 2^{133} compressions.

Joux's attack is clearly not a concrete threat, which is demonstrated ad absurdum: to be applicable, it requires the knowledge of at least two collisions, but any function (resistant or not

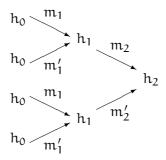


Figure 5.1: Illustration of Joux's technique for 2-collisions, where $compress(h_0, m_1) = compress(h_0, m_1') = h_1$, etc. This technique can apply to BLAKE.

to Joux's attack) for which collisions can be found is broken anyway. Hence this attack only damages non-collision-resistant hash functions.

Kelsey/Schneier's technique

The technique presented by Kelsey and Schneier [29] works only when the compression function admits easily found fixed-points. An advantage over Joux's attack is that the cost of finding a k-collision no longer depends on k. Specifically, for a Merkle-Damgård hash function with n-bit hash values, it makes $3 \cdot 2^{n/2}$ compressions and needs storage for $2^{n/2}$ message blocks (see Fig. 5.2). Colliding messages are long of k blocks. This technique does not apply to BLAKE, because fixed-points cannot be found efficiently, and the counter t foils fixed-point repetition.

$$h_0 \rightarrow \boxed{h_0 \dots h_0} \rightarrow h_j \rightarrow \boxed{h_j \dots \dots h_j} \rightarrow h_n$$

$$h_0 \rightarrow \boxed{h_0 \dots \dots h_0} \rightarrow h_j \rightarrow \boxed{h_j \dots h_j} \rightarrow h_n$$

Figure 5.2: Schematic view of the Kelsey/Schneier multicollision attack on Merkle-Damgård functions. This technique does not apply to BLAKE.

Faster multicollisions

When an iterated hash admits fixed-points and the IV is chosen by the attacker, this technique [2] finds a k-collision in time $2^{n/2}$ and negligible memory, with colliding messages of size $\lceil \log_2 k \rceil$ (see Fig. 5.3. Like the Kelsey/Schneier technique, it is based on the repetition of fixed-points, thus does not apply to BLAKE.

5.5.4 Second preimages

Dean [22, $\S 5.6.3$] and subsequently Kelsey and Schneier [29] showed generic attacks on \mathfrak{n} -bit iterated hashes that find second preimages in significantly less than $2^\mathfrak{n}$ compressions. HAIFA was proven to be resistant to these attacks [23], assuming a strong compression function; this result applies to BLAKE, as a HAIFA-based design. Therefore, no attack on \mathfrak{n} -bit BLAKE can find second-preimages in less than $2^\mathfrak{n}$ trials, unless exploiting the structure of the compression function.

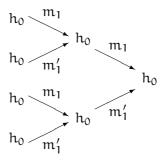


Figure 5.3: Illustration of the faster multicollision, for 2-collisions on Merkle-Damgård hash functions. This technique does not apply to BLAKE.

5.5.5 Side channels

All operations in the BLAKE functions are independent of the input and can be implemented to run in constant time on all platforms (and still be fast). The ChaCha core function was designed to be immune to all kind of side-channel attacks (timing, power analysis, etc.), and BLAKE inherits this property. Side-channel analysis of the eSTREAM finalists also suggests that Salsa20 and ChaCha are immune to side-channel attacks [40].

5.5.6 SAT solvers

Attacks using SAT-solvers consist in describing a security problem in terms of a SAT instance, then solving this instance with an efficient solver. These attacks were used for finding collisions [32] and preimages for (reduced) for MD4 and MD5 [20]. The high complexity of BLAKE and the absence of SAT-solver-based attacks on ChaCha and Salsa20 argues for the resistance of BLAKE to these methods.

5.5.7 Algebraic attacks

Algebraic attacks consist in reducing a security problem to solving a system of equations, then solving this system. The approach is similar to that of SAT-solver attacks, and for similar reasons is unlikely to break BLAKE.

5.6 Dedicated attacks

This section describes several strategies for attacking BLAKE, and justifies their limitations.

5.6.1 Symmetric differences

A sufficient (but not necessary) condition to find a collision on BLAKE is to find two message blocks for which, given same IV's and salts, the corresponding internal states ν and ν' after the sequence of rounds satisfy the relation

$$\nu_i\oplus\nu_{i+8}=\nu_i'\oplus\nu_{i+8}',\ i=0,\dots,7.$$

Put differently, it suffices to find a message difference that leads after the rounds sequence to a difference of the form

$$\begin{pmatrix} v_0 \oplus v_0' & v_1 \oplus v_1' & v_2 \oplus v_2' & v_3 \oplus v_3' \\ v_4 \oplus v_4' & v_5 \oplus v_5' & v_6 \oplus v_6' & v_7 \oplus v_7' \\ v_8 \oplus v_8' & v_9 \oplus v_9' & v_{10} \oplus v_{10}' & v_{11} \oplus v_{11}' \\ v_{12} \oplus v_{12}' & v_{13} \oplus v_{13}' & v_{14} \oplus v_{14}' & v_{15} \oplus v_{15}' \end{pmatrix} = \begin{pmatrix} \Delta_0 & \Delta_1 & \Delta_2 & \Delta_3 \\ \Delta_4 & \Delta_5 & \Delta_6 & \Delta_7 \\ \Delta_0 & \Delta_1 & \Delta_2 & \Delta_3 \\ \Delta_4 & \Delta_5 & \Delta_6 & \Delta_7 \end{pmatrix}.$$

We say that the state has *symmetric* differences. This condition is not necessary for collisions, because there may exist collisions for different salts.

Birthday attack

A birthday attack on ν can be used to find two messages with symmetric differences, that is, a collision for the "top" and "bottom" differences. Since for each pair of messages the collision occurs with probability 2^{-256} , a birthday attack requires about 2^{128} messages. This approach is likely to be a bit faster than a direct birthday attack on the hash function, because here one never computes the finalization of the compression function. The attack may be improved if one finds message differences that give, for example, $\nu_0 \oplus \nu_0' = \nu_8 \oplus \nu_8'$ with probability noticeably higher than 2^{-32} (for BLAKE-32). Such correlations between differences are however very unlikely with the recommended number of rounds.

Backward attack

One can pick two random ν and ν' having symmetric differences, and compute rounds backward for two arbitrary distinct messages. In the end the initial states obtained need

- 1. to have an IV and salt satisfying $h_i \oplus s_{i \bmod 4} = h'_i \oplus s'_{i \bmod 4}$, for $i = 0, \ldots, 7$, which occurs with probability 2^{-256}
- 2. to be valid initial states for a counter 0 < t < 512, which occurs with probability 2^{-128}

Using a birthday strategy, running this attack requires about 2^{256} trials, and finds collisions with different IV's and different salts. If we allow different counters of arbitrary values, then the initial state obtained is valid with probability 2^{-64} , and the attacks runs within $2^{128} \times 2^{64} = 2^{192}$ trials, which is still slower than a direct birthday attack.

5.6.2 Differential attack

BLAKE functions can be attacked if one finds a message difference that gives certain output difference with significantly higher probability than ideally expected. A typical differential attack uses high-probability differentials for the sequence of round functions. An argument against the existence of such differentials is that BLAKE's round function is essentially ChaCha's "double-round", whose differential behavior has been intensively studied without real success; in [3].

Attacks on ChaCha are based on the existence of truncated differentials after three steps (that is, one and a half BLAKE round) [3]. These differentials have a 1-bit input difference and a 1-bit output difference; namely, flipping certain bits gives non-negligible biases in certain output bits. No truncated differential was found through four steps (two BLAKE rounds). This suggests that differentials in BLAKE with input difference in the IV or the salt cannot be found for more than two rounds. An input difference in the message spreads even more, because the difference affects the state through each round of the function.

Rumba [8] is a compression function based on the stream cipher Salsa20; contrary to BLAKE, the message is put in the initial state and no data is input during the rounds iteration. Attacks on Rumba in [3] are based on the identification of a linear approximation through three steps, and the use of message modification techniques to increase the probability of finding compliant messages. Rumba is based on Salsa20, not on ChaCha, and thus such differentials are likely to have much lower probability with ChaCha. With its ten rounds (20 steps), BLAKE is very unlikely to be attacked with such techniques.

5.6.3 Slide attack

Slide attacks were originally proposed to attack block ciphers [11,12], and recently were applied in some sense to hash functions [38]. Here we show how to apply the idea to attack a modified variant of BLAKE's compression function.

Suppose all the permutations σ_i are equal (to, say, the identity). Then for a message such that $m_0 = \cdots = m_{15}$, the sequence of rounds is a repeated application of the same permutation on the internal state, because for each G_i , the value $(m_{\sigma_r(2i)} \oplus c_{\sigma_r(2i+1)})$ is now independent of the round index r. The idea of the attack is to use 256 bits of freedom of the message to have, after one round, an internal state ν' such that $h_i \oplus s_{i \bmod 4} = h_i' \oplus s_{i \bmod 4}'$, for h' and s' derived from ν' according to the initialization rule. The state obtained will be valid with probability 2^{-64} . Then, for the same message and the (r-1)-round function, we get a collision after the finalization process, with different IV, salt, and counter. Runtime is 2^{64} trials, to find collisions with two different versions of the compression function. For the full version (with nontrivial permutations), this attack cannot work for more than two rounds.

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A Round function example

We give an example of computation by the BLAKE-32 round function. At the first round $G_0(\nu_0^-,\nu_4^-,\nu_8^-,\nu_{12}^-)$ computes

where 85A308D3 = $c_{\sigma_0(2\times 0+1)}=c_1$ and 243F6A88 = $c_{\sigma_0(2\times 0)}=c_0$. Then $G_1(\nu_1\ ,\nu_5\ ,\nu_9\ ,\nu_{13})$ computes

$$v_{1} \leftarrow v_{1} + v_{5} + (m_{2} \oplus 03707344)$$
 $v_{13} \leftarrow (v_{13} \oplus v_{1}) \gg 16$
 $v_{9} \leftarrow v_{9} + v_{13}$
 $v_{5} \leftarrow (v_{5} \oplus v_{9}) \gg 12$
 $v_{1} \leftarrow v_{1} + v_{5} + (m_{3} \oplus 13198A2E)$
 $v_{13} \leftarrow (v_{13} \oplus v_{1}) \gg 8$
 $v_{9} \leftarrow v_{9} + v_{13}$
 $v_{5} \leftarrow (v_{5} \oplus v_{9}) \gg 7$

and so on until $G_7(v_3, v_4, v_9, v_{14})$, which computes

$$v_{3} \leftarrow v_{3} + v_{4} + (m_{14} \oplus B5470917)$$
 $v_{14} \leftarrow (v_{14} \oplus v_{3}) \gg 16$
 $v_{9} \leftarrow v_{9} + v_{14}$
 $v_{4} \leftarrow (v_{4} \oplus v_{9}) \gg 12$
 $v_{3} \leftarrow v_{3} + v_{4} + (m_{15} \oplus 3F84D5B5)$
 $v_{14} \leftarrow (v_{14} \oplus v_{3}) \gg 8$
 $v_{9} \leftarrow v_{9} + v_{14}$
 $v_{4} \leftarrow (v_{4} \oplus v_{9}) \gg 7$

After $G_7(v_3, v_4, v_9, v_{14})$, the second round starts. Because of the round-dependent permuta-

tions, $G_0(\nu_0$, ν_4 , ν_8 , $\nu_{12})$ now uses the permutation σ_1 instead of σ_0 , and thus computes

Above, $14 = \sigma_1(2 \times 0) = \sigma_1(0)$, $10 = \sigma_1(2 \times 0 + 1) = \sigma_1(1)$, BE5466CF $= c_{10}$, and 3F84D5B5 $= c_{14}$. Applying similar rules, column steps and diagonal steps continue until the tenth round, which uses the permutation σ_9 .

B Source code

B.1 VHDL

We give our VHDL code computing the compression function of BLAKE-32 with the [8G] architecture. We split the implementation into 7 vhd files: blake32, blake32Pkg, initialization, roundreg, gcomp, finalization, and controller:

```
File blake32.vhd
```

```
library ieee;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use std.textio.all;
use ieee.std_logic_textio.all;
use work.blake32Pkg.all;
entity blake32 is
   port (
     CLKxCI : in std_logic;
     RSTxRBI : in std_logic;
     MxDI : in std_logic_vector(WWIDTH*16-1 downto 0);
     HxDI : in std_logic_vector(WWIDTH*8-1 downto 0);
     SxDI : in std_logic_vector(WWIDTH*4-1 downto 0);
     TxDI : in std_logic_vector(WWIDTH*2-1 downto 0);
     HxDO : out std_logic_vector(WWIDTH*8-1 downto 0);
     InENxSI : in std_logic;
     OutENxSO : out std_logic
     );
end blake32:
architecture hash of blake32 is
   component controller
     port (
       CLKxCI : in std_logic;
        RSTxRBI : in std_logic;
        VALIDINxSI : in std_logic;
        VALIDOUTxSO : out std_logic;
       ROUNDxSO : out unsigned(3 downto 0)
   end component;
   component initialization
     port (
       HxDI : in std_logic_vector(WWIDTH*8-1 downto 0);
       SxDI : in std_logic_vector(WWIDTH*4-1 downto 0);
        TxDI : in std_logic_vector(WWIDTH*2-1 downto 0);
        VxD0 : out std_logic_vector(WWIDTH*16-1 downto 0)
   end component;
   component roundreg
```

```
port (
       CLKxCI : in std_logic;
       RSTxRBI : in std_logic;
       WEIxSI : in std_logic;
       ROUNDxSI : in unsigned(3 downto 0);
       VxDI : in std_logic_vector(WWIDTH*16-1 downto 0);
       MxDI : in std_logic_vector(WWIDTH*16-1 downto 0);
       VxD0 : out std_logic_vector(WWIDTH*16-1 downto 0)
   end component;
   component finalization
     port (
       VxDI : in std_logic_vector(WWIDTH*16-1 downto 0);
       HxDI : in std_logic_vector(WWIDTH*8-1 downto 0);
       SxDI : in std_logic_vector(WWIDTH*4-1 downto 0);
       HxDO : out std_logic_vector(WWIDTH*8-1 downto 0)
   end component;
   signal VxD, VFINALxD : std_logic_vector(WWIDTH*16-1 downto 0);
   signal ROUNDxS : unsigned(3 downto 0);
begin -- hash
   -- CONTROLLER
   u\_controller: controller
     port map (
       CLKxCI => CLKxCI,
       RSTxRBI => RSTxRBI,
       VALIDINxSI => InENxSI,
       VALIDOUTxSO => OutENxSO,
       ROUNDxSO => ROUNDxS
       );
   -- INITIALIZATION
   ______
   u_initialization: initialization
     port map (
       HxDI => HxDI,
       SxDI => SxDI,
       TxDI => TxDI,
       VxDO => VxD
       ):
   u_roundreg: roundreg
     port map (
       CLKxCI => CLKxCI,
       RSTxRBI => RSTxRBI,
       WEIxSI => InENxSI,
       ROUNDxSI => ROUNDxS,
       VxDI => VxD,
       MxDI => MxDI,
       VxDO => VFINALxD
       );
   -- FINALIZATION
```

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```
u_finalization: finalization
     port map (
       VxDI => VFINALxD,
       HxDI => HxDI,
       SxDI => SxDI,
       HxDO => HxDO
end hash;
File blake32Pkg.vhd
library ieee;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use std.textio.all;
use ieee.std_logic_textio.all;
package blake32Pkg is
   constant WWIDTH : integer := 32; -- WORD WIDTH
   constant NROUND : integer := 10; -- ROUND NUMBER
   -- c Constants
   ______
   type c_const is array (0 to 15) of std_logic_vector(31 downto 0);
   constant C : c_{const} := ((x"243F6A88"), (x"85A308D3"),
                           (x"13198A2E"), (x"03707344"),
                           (x"A4093822"), (x"299F31D0"),
                           (x"082EFA98"), (x"EC4E6C89"),
                           (x"452821E6"), (x"38D01377"),
                           (x"BE5466CF"), (x"34E90C6C"),
                           (x"COAC29B7"), (x"C97C50DD"),
                           (x"3F84D5B5"), (x"B5470917"));
   -- o Permutations
   ______
   type perm is array (0 to 9, 0 to 15) of integer;
   constant PMATRIX : perm := ((0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15),
                             (14, 10, 4, 8, 9, 15, 13, 6, 1, 12, 0, 2, 11, 7, 5, 3),
                             (11, 8, 12, 0, 5, 2, 15, 13, 10, 14, 3, 6, 7, 1, 9, 4),
                             (7, 9, 3, 1, 13, 12, 11, 14, 2, 6, 5, 10, 4, 0, 15, 8),
                             (9, 0, 5, 7, 2, 4, 10, 15, 14, 1, 11, 12, 6, 8, 3, 13),
                             (2, 12, 6, 10, 0, 11, 8, 3, 4, 13, 7, 5, 15, 14, 1, 9),
                             (12, 5, 1, 15, 14, 13, 4, 10, 0, 7, 6, 3, 9, 2, 8, 11),
                             (13, 11, 7, 14, 12, 1, 3, 9, 5, 0, 15, 4, 8, 6, 2, 10),
                             (6, 15, 14, 9, 11, 3, 0, 8, 12, 2, 13, 7, 1, 4, 10, 5),
                             (10, 2, 8, 4, 7, 6, 1, 5, 15, 11, 9, 14, 3, 12, 13, 0));
end blake32Pkg;
File initialization. vhd
library ieee;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use std.textio.all;
use ieee.std_logic_textio.all;
use work.blake32Pkg.all;
```

```
entity initialization is
   port (
     HxDI : in std_logic_vector(WWIDTH*8-1 downto 0);
     SxDI : in std_logic_vector(WWIDTH*4-1 downto 0);
     TxDI : in std_logic_vector(WWIDTH*2-1 downto 0);
     VxD0 : out std_logic_vector(WWIDTH*16-1 downto 0)
     );
end initialization;
architecture hash of initialization is
begin -- hash
   VxDO(WWIDTH*16-1 downto WWIDTH*8) <= HxDI;</pre>
   VxDO(WWIDTH*8-1 downto WWIDTH*7) <= SxDI(WWIDTH*4-1 downto WWIDTH*3) xor C(0);</pre>
   VxDO(WWIDTH*7-1 downto WWIDTH*6) <= SxDI(WWIDTH*3-1 downto WWIDTH*2) xor C(1);</pre>
   VxDO(WWIDTH*6-1 downto WWIDTH*5) <= SxDI(WWIDTH*2-1 downto WWIDTH) xor C(2);</pre>
   VxDO(WWIDTH*5-1 downto WWIDTH*4) <= SxDI(WWIDTH-1 downto 0) xor C(3);</pre>
   VxDO(WWIDTH*4-1 downto WWIDTH*3) <= TxDI(WWIDTH*2-1 downto WWIDTH) xor C(4);</pre>
   VxDO(WWIDTH*3-1 downto WWIDTH*2) <= TxDI(WWIDTH*2-1 downto WWIDTH) xor C(5);</pre>
   VxDO(WWIDTH*2-1 downto WWIDTH) <= TxDI(WWIDTH-1 downto 0) xor C(6);</pre>
   VxDO(WWIDTH-1 downto 0) <= TxDI(WWIDTH-1 downto 0) xor C(7);</pre>
end hash;
File roundreg. vhd
library ieee;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use std.textio.all;
use ieee.std_logic_textio.all;
use work.blake32Pkg.all;
entity roundreg is
   port (
     CLKxCI : in std_logic;
     RSTxRBI : in std_logic;
     WEIxSI : in std_logic;
     ROUNDxSI : in unsigned(3 downto 0);
     VxDI : in std_logic_vector(WWIDTH*16-1 downto 0);
     MxDI : in std_logic_vector(WWIDTH*16-1 downto 0);
     VxD0 : out std_logic_vector(WWIDTH*16-1 downto 0)
     );
end roundreg;
architecture hash of roundreg is
   component gcomp
     port (
        AxDI : in std_logic_vector(WWIDTH-1 downto 0);
       BxDI : in std_logic_vector(WWIDTH-1 downto 0);
        CxDI : in std_logic_vector(WWIDTH-1 downto 0);
       DxDI : in std_logic_vector(WWIDTH-1 downto 0);
       MxDI : in std_logic_vector(WWIDTH*2-1 downto 0);
       KxDI : in std_logic_vector(WWIDTH*2-1 downto 0);
        AxDO : out std_logic_vector(WWIDTH-1 downto 0);
        BxDO : out std_logic_vector(WWIDTH-1 downto 0);
        CxDO : out std_logic_vector(WWIDTH-1 downto 0);
       DxDO : out std_logic_vector(WWIDTH-1 downto 0)
        );
   end component;
```

```
type SUBT16 is array (15 downto 0) of std_logic_vector(WWIDTH-1 downto 0);
   signal VxDN, VxDP, MxD : SUBT16;
   signal GOMxD, GOKxD, G4MxD, G4KxD : std_logic_vector(WWIDTH*2-1 downto 0);
   signal G1MxD, G1KxD, G5MxD, G5KxD : std_logic_vector(WWIDTH*2-1 downto 0);
   signal G2MxD, G2KxD, G6MxD, G6KxD : std_logic_vector(WWIDTH*2-1 downto 0);
   signal G3MxD, G3KxD, G7MxD, G7KxD : std_logic_vector(WWIDTH*2-1 downto 0);
   signal GOAOxD, GOBOxD, GOCOxD, GODOxD : std_logic_vector(WWIDTH-1 downto 0);
   signal G1AOxD, G1BOxD, G1COxD, G1DOxD : std_logic_vector(WWIDTH-1 downto 0);
   signal G2AOxD, G2BOxD, G2COxD, G2DOxD : std_logic_vector(WWIDTH-1 downto 0);
   signal G3AOxD, G3BOxD, G3COxD, G3DOxD: std_logic_vector(WWIDTH-1 downto 0);
   signal G4AOxD, G4BOxD, G4COxD, G4DOxD : std_logic_vector(WWIDTH-1 downto 0);
   signal G5A0xD, G5B0xD, G5C0xD, G5D0xD : std_logic_vector(WWIDTH-1 downto 0);
   signal G6AOxD, G6BOxD, G6COxD, G6DOxD : std_logic_vector(WWIDTH-1 downto 0);
   signal G7AOxD, G7BOxD, G7COxD, G7DOxD: std_logic_vector(WWIDTH-1 downto 0);
begin -- hash
   p_unform: for i in 15 downto 0 generate
     MxD(15-i) <= MxDI(WWIDTH*(i+1)-1 downto WWIDTH*i);</pre>
   end generate p_unform;
   VxDO <= VxDP(0) & VxDP(1) & VxDP(2) & VxDP(3) &
               VxDP(4) & VxDP(5) & VxDP(6) & VxDP(7) &
               VxDP(8) & VxDP(9) & VxDP(10) & VxDP(11) &
               VxDP(12) & VxDP(13) & VxDP(14) & VxDP(15);
   -- MEMORY INPUTS
   ______
   p_inmem: process (G4AOxD, G4BOxD, G4COxD, G4DOxD, G5AOxD, G5BOxD, G5COxD,
                       G5DOxD, G6AOxD, G6BOxD, G6COxD, G6DOxD, G7AOxD, G7BOxD,
                       G7COxD, G7DOxD, VxDI, VxDP, WEIxSI)
   begin -- process p_inmem
     VxDN <= VxDP;
     if WEIxSI = '1' then
       for i in 15 downto 0 loop
         VxDN(15-i) <= VxDI(WWIDTH*(i+1)-1 downto WWIDTH*i);</pre>
       end loop;
     else
       VxDN(0) <= G4A0xD;
       VxDN(5) <= G4B0xD;</pre>
       VxDN(10) <= G4C0xD;
       VxDN(15) <= G4D0xD;
       VxDN(1) <= G5A0xD;
       VxDN(6)  <= G5B0xD;
       VxDN(11) <= G5COxD;
       VxDN(12) <= G5D0xD;</pre>
       VxDN(2) <= G6A0xD;
       VxDN(7) <= G6B0xD;</pre>
       VxDN(8) <= G6COxD;
       VxDN(13) <= G6D0xD;</pre>
       VxDN(3) <= G7A0xD;
       VxDN(4) <= G7B0xD;</pre>
       VxDN(9) <= G7C0xD;</pre>
       VxDN(14) <= G7D0xD;</pre>
     end if;
```

```
end process p_inmem;
______
-- G INPUTS
p_outmem: process (MxD, ROUNDxSI)
begin -- process p_outmem
  GOMxD <= MxD(PMATRIX(to_integer(ROUNDxSI), 0)) & MxD(PMATRIX(to_integer(ROUNDxSI), 1));</pre>
  G1MxD <= MxD(PMATRIX(to_integer(ROUNDxSI), 2)) & MxD(PMATRIX(to_integer(ROUNDxSI), 3));</pre>
  G2MxD <= MxD(PMATRIX(to_integer(ROUNDxSI), 4)) & MxD(PMATRIX(to_integer(ROUNDxSI), 5));</pre>
  G3MxD <= MxD(PMATRIX(to_integer(ROUNDxSI), 6)) & MxD(PMATRIX(to_integer(ROUNDxSI), 7));</pre>
  G4MxD <= MxD(PMATRIX(to_integer(ROUNDxSI), 8)) & MxD(PMATRIX(to_integer(ROUNDxSI), 9));
  G5MxD <= MxD(PMATRIX(to_integer(ROUNDxSI), 10)) & MxD(PMATRIX(to_integer(ROUNDxSI), 11));</pre>
  G6MxD <= MxD(PMATRIX(to_integer(ROUNDxSI), 12)) & MxD(PMATRIX(to_integer(ROUNDxSI), 13));</pre>
  G7MxD <= MxD(PMATRIX(to_integer(ROUNDxSI), 14)) & MxD(PMATRIX(to_integer(ROUNDxSI), 15));
  GOKxD <= C(PMATRIX(to_integer(ROUNDxSI), 1)) & C(PMATRIX(to_integer(ROUNDxSI), 0));</pre>
  G1KxD <= C(PMATRIX(to_integer(ROUNDxSI), 3)) & C(PMATRIX(to_integer(ROUNDxSI), 2));</pre>
  G2KxD <= C(PMATRIX(to_integer(ROUNDxSI), 5)) & C(PMATRIX(to_integer(ROUNDxSI), 4));</pre>
  G3KxD <= C(PMATRIX(to_integer(ROUNDxSI), 7)) & C(PMATRIX(to_integer(ROUNDxSI), 6));</pre>
  G4KxD <= C(PMATRIX(to_integer(ROUNDxSI), 9)) & C(PMATRIX(to_integer(ROUNDxSI), 8));
  G5KxD <= C(PMATRIX(to_integer(ROUNDxSI), 11)) & C(PMATRIX(to_integer(ROUNDxSI), 10));
  G6KxD <= C(PMATRIX(to_integer(ROUNDxSI), 13)) & C(PMATRIX(to_integer(ROUNDxSI), 12));
  G7KxD <= C(PMATRIX(to_integer(ROUNDxSI), 15)) & C(PMATRIX(to_integer(ROUNDxSI), 14));
end process p_outmem;
              ______
-- G BLOCKS
              ______
u_gcomp0: gcomp
  port map (
    AxDI => VxDP(0), BxDI => VxDP(4), CxDI => VxDP(8), DxDI => VxDP(12), MxDI => GOMxD,
    KxDI => GOKxD, AxDO => GOAOxD, BxDO => GOBOxD, CxDO => GOCOxD, DxDO => GODOxD
u_gcomp1: gcomp
  port map (
    AxDI => VxDP(1), BxDI => VxDP(5), CxDI => VxDP(9), DxDI => VxDP(13), MxDI => G1MxD,
    KxDI => G1KxD, AxDO => G1AOxD, BxDO => G1BOxD, CxDO => G1COxD, DxDO => G1DOxD
u_gcomp2: gcomp
  port map (
    AxDI => VxDP(2), BxDI => VxDP(6), CxDI => VxDP(10), DxDI => VxDP(14), MxDI => G2MxD,
    \texttt{KxDI} = \texttt{G2KxD}, \texttt{AxDO} = \texttt{G2A0xD}, \texttt{BxDO} = \texttt{G2B0xD}, \texttt{CxDO} = \texttt{G2C0xD}, \texttt{DxDO} = \texttt{G2D0xD}
    );
u_gcomp3: gcomp
  port map (
    AxDI => VxDP(3), BxDI => VxDP(7), CxDI => VxDP(11), DxDI => VxDP(15), MxDI => G3MxD,
    KxDI => G3KxD, AxDO => G3AOxD, BxDO => G3BOxD, CxDO => G3COxD, DxDO => G3DOxD
u_gcomp4: gcomp
    AxDI => GOAOxD, BxDI => G1BOxD, CxDI => G2COxD, DxDI => G3DOxD, MxDI => G4MxD,
    \texttt{KxDI} = \texttt{S4KxD}, \texttt{AxD0} = \texttt{S4A0xD}, \texttt{BxD0} = \texttt{S4B0xD}, \texttt{CxD0} = \texttt{S4C0xD}, \texttt{DxD0} = \texttt{S4D0xD}
u_gcomp5: gcomp
```

AxDI => G1AOxD, BxDI => G2BOxD, CxDI => G3COxD, DxDI => G0DOxD, MxDI => G5MxD,

port map (

```
KxDI => G5KxD, AxDO => G5AOxD, BxDO => G5BOxD, CxDO => G5COxD, DxDO => G5DOxD
       );
   u_gcomp6: gcomp
     port map (
       AxDI => G2AOxD, BxDI => G3BOxD, CxDI => G0COxD, DxDI => G1DOxD, MxDI => G6MxD,
       KxDI => G6KxD, AxDO => G6A0xD, BxDO => G6B0xD, CxDO => G6C0xD, DxDO => G6D0xD
   u_gcomp7: gcomp
     port map (
       AxDI => G3AOxD, BxDI => G0BOxD, CxDI => G1COxD, DxDI => G2DOxD, MxDI => G7MxD,
       KxDI => G7KxD, AxDO => G7AOxD, BxDO => G7BOxD, CxDO => G7COxD, DxDO => G7DOxD
   -- v MEMORY
   p_mem: process (CLKxCI, RSTxRBI)
   begin -- process p_vmem
     if RSTxRBI = '0' then -- asynchronous reset (active low)
       VxDP <= (others => '0'));
     elsif CLKxCI'event and CLKxCI = '1' then -- rising clock edge
       VxDP <= VxDN;
     end if;
   end process p_mem;
end hash;
File gcomp. vhd
library ieee;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use std.textio.all;
use ieee.std_logic_textio.all;
use work.blake32Pkg.all;
entity gcomp is
   port (
     AxDI : in std_logic_vector(WWIDTH-1 downto 0);
     BxDI : in std_logic_vector(WWIDTH-1 downto 0);
     CxDI : in std_logic_vector(WWIDTH-1 downto 0);
     DxDI : in std_logic_vector(WWIDTH-1 downto 0);
     MxDI : in std_logic_vector(WWIDTH*2-1 downto 0);
     KxDI : in std_logic_vector(WWIDTH*2-1 downto 0);
     AxDO : out std_logic_vector(WWIDTH-1 downto 0);
     BxDO : out std_logic_vector(WWIDTH-1 downto 0);
     CxDO : out std_logic_vector(WWIDTH-1 downto 0);
     DxDO : out std_logic_vector(WWIDTH-1 downto 0)
     );
end gcomp;
architecture hash of gcomp is
   signal T1, T4, T7, T10 : unsigned(WWIDTH-1 downto 0);
   signal T2, T3, T5, T6 : std_logic_vector(WWIDTH-1 downto 0);
   signal T8, T9, T11, T12 : std_logic_vector(WWIDTH-1 downto 0);
   signal TK1, TK2 : std_logic_vector(WWIDTH-1 downto 0);
begin -- hash
   TK1 <= MxDI(WWIDTH*2-1 downto WWIDTH) xor KxDI(WWIDTH*2-1 downto WWIDTH);
   T1 <= unsigned(AxDI) + unsigned(BxDI) + unsigned(TK1);
```

```
T2 <= std_logic_vector(T1) xor DxDI;
   T3 <= T2(15 downto 0) & T2(WWIDTH-1 downto 16);
   T4 <= unsigned(CxDI) + unsigned(T3);
   T5 <= std_logic_vector(T4) xor BxDI;
   T6 <= T5(11 downto 0) & T5(WWIDTH-1 downto 12);
   TK2 <= MxDI(WWIDTH-1 downto 0) xor KxDI(WWIDTH-1 downto 0);</pre>
   T7 <= T1 + unsigned(T6) + unsigned(TK2);
   T8 <= std_logic_vector(T7) xor T3;
   T9 <= T8(7 downto 0) & T8(WWIDTH-1 downto 8);
   T10 <= T4 + unsigned(T9);
   T11 <= std_logic_vector(T10) xor T6;</pre>
   T12 \ll T11(6 \text{ downto 0}) \& T11(WWIDTH-1 \text{ downto 7});
   AxDO <= std_logic_vector(T7);</pre>
   BxD0 <= T12;
   CxDO <= std_logic_vector(T10);</pre>
   DxDO <= T9;
end hash;
File finalization. vhd
library ieee;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use std.textio.all;
use ieee.std_logic_textio.all;
use work.blake32Pkg.all;
entity finalization is
   port (
     VxDI : in std_logic_vector(WWIDTH*16-1 downto 0);
     HxDI : in std_logic_vector(WWIDTH*8-1 downto 0);
     SxDI : in std_logic_vector(WWIDTH*4-1 downto 0);
     HxD0 : out std_logic_vector(WWIDTH*8-1 downto 0)
     );
end finalization;
architecture hash of finalization is
    type SUB4 is array (3 downto 0) of std_logic_vector(WWIDTH-1 downto 0);
   type SUB8 is array (7 downto 0) of std_logic_vector(WWIDTH-1 downto 0);
   type SUB16 is array (15 downto 0) of std_logic_vector(WWIDTH-1 downto 0);
   signal SINxD : SUB4;
   signal HINxD, HOUTxD : SUB8;
   signal VxD : SUB16;
begin -- hash
   p\_unform4: for i in 0 to 3 generate
     SINxD(i) <= SxDI(WWIDTH*(i+1)-1 downto WWIDTH*i);</pre>
   end generate p_unform4;
   p_unform8: for i in 0 to 7 generate
     HINxD(i) <= HxDI(WWIDTH*(i+1)-1 downto WWIDTH*i);</pre>
     HxDO(WWIDTH*(i+1)-1 downto WWIDTH*i) <= HOUTxD(i);</pre>
   end generate p_unform8;
   p_unform16: for i in 0 to 15 generate
     VxD(i) <= VxDI(WWIDTH*(i+1)-1 downto WWIDTH*i);</pre>
   end generate p_unform16;
```

```
HOUTxD(0) <= HINxD(0) xor VxD(0) xor VxD(8) xor SINxD(0);</pre>
   HOUTxD(1) <= HINxD(1) xor VxD(1) xor VxD(9) xor SINxD(1);</pre>
   HOUTxD(2) <= HINxD(2) xor VxD(2) xor VxD(10) xor SINxD(2);</pre>
   HOUTxD(3) <= HINxD(3) xor VxD(3) xor VxD(11) xor SINxD(3);</pre>
    HOUTxD(4) <= HINxD(4) xor VxD(4) xor VxD(12) xor SINxD(0);</pre>
    \mathtt{HOUTxD}(5) <= \mathtt{HINxD}(5) \ \mathtt{xor} \ \mathtt{VxD}(5) \ \mathtt{xor} \ \mathtt{VxD}(13) \ \mathtt{xor} \ \mathtt{SINxD}(1);
    HOUTxD(6) <= HINxD(6) xor VxD(6) xor VxD(14) xor SINxD(2);</pre>
    HOUTxD(7) <= HINxD(7) xor VxD(7) xor VxD(15) xor SINxD(3);</pre>
end hash;
File controller.vhd
library ieee;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use std.textio.all;
use ieee.std_logic_textio.all;
use work.blake32Pkg.all;
    entity controller is
    port (
      CLKxCI : in std_logic;
      RSTxRBI : in std_logic;
      VALIDINxSI : in std_logic;
      VALIDOUTxSO : out std_logic;
      ROUNDxSO : out unsigned(3 downto 0)
      );
end controller;
architecture hash of controller is
    type state is (idle, round, fin);
    signal STATExDP, STATExDN : state;
    signal ROUNDxDP, ROUNDxDN : unsigned(3 downto 0);
begin -- hash
    ROUNDxSO <= ROUNDxDP;</pre>
    fsm: process (ROUNDxDP, STATExDP, VALIDINxSI)
    begin -- process fsm
      VALIDOUTxSO <= '0';</pre>
      ROUNDxDN <= (others => '0');
      case STATExDP is
        when idle =>
           if VALIDINxSI = '1' then
            STATExDN <= round;
             STATExDN <= idle;
           end if;
        when round =>
           if \ ROUNDxDP < NROUND-1 \ then
             ROUNDxDN <= ROUNDxDP + 1;</pre>
             STATExDN <= round;
          else
```

```
STATExDN <= fin;
         end if;
       when fin =>
        VALIDOUTxSO <= '1';</pre>
        {\tt STATExDN} <= {\tt idle};
        ______
       when others =>
        STATExDN <= idle;
       end case;
   end process fsm;
   process (CLKxCI, RSTxRBI)
   begin -- process
     if RSTxRBI = '0' then -- asynchronous reset (active low)
       STATExDP <= idle;</pre>
      ROUNDxDP <= (others => '0');
     elsif CLKxCI'event and CLKxCI = '1' then -- rising clock edge
       STATExDP <= STATExDN;
       ROUNDxDP <= ROUNDxDN;</pre>
       end if;
   end process;
end hash;
```

B.2 PIC assembly

We give our assembly code computing the round function of BLAKE-32.

```
; round function of BLAKE32
                                                                                                                                           ; indirect adress register FSRO used for accessing m
                                                                                                                                          ; FSR1 used for accessing c
do_Gi
                                                            clrf FSR1H
                                                                                                                                         ; stays zero al the time
                                                                                                                                         ; only lower adress range is used for cts address
                                                            movlw h'01'
                                                                                                                                        ; table m starts at equ H'110'
                                                            movWF FSROH
                                                                                                                                       ; so using FSRO we need to set highbyte correct
                                                            movFF i,pointer2mc
                                                                                                                                       ; use i
                                                                                                                                        ; prepare CARRYbit for *2
                                                            bcf STATUS, C
                                                                                                                                        ; 2*i
                                                            rlcF pointer2mc
                                                            movF pointer2mc
                                                                                                                                        ; load pointer into w
                                                           addWF r,w ; ADD r (permutation offset in table)
movWF pointer2mc ; ..save it back is a fine of the second of the s
                                                            movwf TBLPTRH
                                                            rlncf pointer2mc, w
                                                            movwf TBLPTRL
                                                                                                                                          ; table read here into TABLAT
                                                            tblrd*
                                                            movff TABLAT, FSROL
                                                                                                                                        ; move adress to pointer
                                                            movFF INDFO,tmpXOR_lo
                                                                                                                                        ; access content of m signum_r(2i) low byte loaded
                                                            movFF PREINCO,tmpXOR_ml ; preincrement pointer, access midlowbyte
                                                            movFF PREINCO,tmpXOR_mh ; preincrement pointer, access midhighbyte
                                                            movFF PREINCO,tmpXOR_hi ; preincrement pointer, access highbyte
```

term_a1_lowbyte

```
incF pointer2mc
movF pointer2mc
                     movlw high permut_table_c ; find c signum_r (2i+1)lowbyte adress
                     movwf TBLPTRH
                     rlncf pointer2mc, w
                     movwf TBLPTRL
                     tblrd*
                                                 ; table read here into TABLAT
                     movff TABLAT, FSR1L
                                                ; move adress to pointer
                     movF INDF1
                                                 ; content of c signum_r(2i+1) now in working reg
                     xorWF tmpXOR_lo,w
                                                ; lowest byte [m signum_r (2i) XOR c signum_r (2i+1)]
                                                 ; ADD b with carry
                     addWFC b_lo,w
                                                ; IF carrybit =1 ...
                     btfsc STATUS, C
                                                ; then ... add carry
                     incF tmpXOR_ml
                                                ; IF carrybit =1 ...
                     btfsc STATUS, C
                                                ; then ... add carry
                     incF tmpXOR_mh
                     btfsc STATUS, C
                                               ; IF carrybit =1 ...
                     incF tmpXOR_hi
                                                 ; then ... add carry
                                            ; ADD a, place result
; IF carrybit =1 ...
; then ... add carry
; IF carrybit =1 ...
; then ... add carry
; IF carrybit =1 ...
; then ... add carry
                     addWFC a_lo,f
                                                ; ADD a, place result in a
                     btfsc STATUS, C
                     incF tmpXOR_ml
                     btfsc STATUS, C
                     incF tmpXOR_mh
                     btfsc STATUS, C
                     incF tmpXOR_hi
                                                ; then ... add carry
term_a1_midlowbyte
                     movF PREINC1
                                                ; content of c signum_r (2i+1) midlow byte loaded in w
                                            ; content of c signum_r (2i+1) midlow byte loaded in ; midlow byte [m signum_r (2i) XOR c signum_r (2i+1)]
                     xorWF tmpXOR_ml,w
                     addWFC b_ml,w
                                                ; ADD b with carry
                                                ; IF carrybit =1 ...
                     btfsc STATUS, C
                     incF tmpXOR_mh
                                                ; then ... add carry
                     btfsc STATUS, C
                                             ; IF carrybit =1 ...
                     incF tmpXOR_hi
                                                ; then ... add carry
                                              ; ADD a, place result in a
                     addWFC a_ml,f
                                                ; IF carrybit =1 ...
                     btfsc STATUS, C
                                              ; then ... add carry
; IF carrybit =1 ...
                     incF tmpXOR_mh
                     btfsc STATUS, C
                     incF tmpXOR_hi
                                                 ; then ... add carry
term_a1_midhighbyte
                                                ; content of c signum_r (2i+1) midhigh byte loaded in w
                     movF PREINC1
                     xorWF tmpXOR_mh,w
                                                 ; midhigh byte [m signum (2i) XOR c signum (2i+1)]
                     addWFC b_mh,w
                                                 ; ADD b with carry
                     btfsc STATUS, C
                                                 ; IF carrybit =1 ...
                     incF tmpXOR_hi
                                                ; then ... add carry
                     addWFC a_mh,f
                                                ; ADD a, place result in a
                     btfsc STATUS, C
                                             ; IF carrybit =1 ...
; then ... add carry
                     incF tmpXOR_hi
```

; pointer now (2i+1) ; load pointer into w

```
term_a1_highbyte
                    movF PREINC1
                                              ; content of c signum_r (2i+1) high byte loaded in w
                                               ; highest byte [m signum (2i) XOR c signum (2i+1)]
                    xorWF tmpXOR_hi,w
                    addWFC b_hi,w
                                               ; ADD b with carry, but carry disapears in black hole
                    addWFC a_hi,f
                                               ; ADD a, place result in a
term_d1
                                               ;... next is d = d xor a \ll 16
                    call compute_dxora
                    movFF d_hi,tmpXOR_hi
                                               ; rotate 16 is actually only swapping
                    movFF d_ml,d_hi
                    movFF tmpXOR_hi,d_ml
                    movFF d_mh,tmpXOR_mh
                    movFF d_lo,d_mh
                    movFF tmpXOR_mh,d_lo
term_c1
                    call compute_c
term_b1
                                               ;... next is b = b xor c \ll 12
                    call compute_bxorc
                                               ; now rotate left 12 positions
                    bcf STATUS, C
                                               ; prepare Carry flag with 0
                    btfsc b_ml,7
                                               ; IF bit 7 of ml-byte
                    bsf STATUS, C
                                              ; THEN prepare Carry with 1
                    rlcF b_hi
                    rlcF b_ml
                    rlcF b_hi
                    rlcF b_ml
                    rlcF b_hi
                    rlcF b_ml
                    rlcF b_hi
                    rlcF b_ml
                    bcf STATUS, C
                                             ; prepare Carry flag with 0
                    btfsc b_lo,7
                                              ; IF bit 7 of ml-byte
                    bsf STATUS, C
                                              ; THEN prepare Carry with 1
                    rlcF b_mh
                    rlcF b_lo
                    rlcF b_mh
                    rlcF b_lo
                    rlcF b_mh
                    rlcF b_lo
                    rlcF b_mh
                    rlcF b_lo
term_a2
                    movF pointer2mc
                                       ; load pointer into w [now (2i+1)]
                    movlw high permut_table_m \,\, ; ...and use it here to find address of current m \,
                    movwf TBLPTRH
                    rlncf pointer2mc, w
                    movwf TBLPTRL
                    tblrd*
                                               ; table read here into TABLAT
                    movff TABLAT, FSROL
                                               ; move adress to pointer
                    movFF INDFO,tmpXOR_lo
                                               ; access content of m signum_r(2i) low byte loaded
                    movFF PREINCO,tmpXOR_ml
                                               ; preincrement pointer, access midlowbyte
```

movFF PREINCO,tmpXOR_mh
movFF PREINCO,tmpXOR_hi

; preincrement pointer, access midhighbyte

; preincrement pointer, access highbyte

```
term_a2_lowbyte
```

```
decF pointer2mc
movF pointer2mc
                                               ; pointer now (2i)
                                                ; load pointer into w
                     movlw high permut_table_c ; find c signum_r (2i)lowbyte adress
                     movwf TBLPTRH
                     rlncf pointer2mc, w
                     movwf TBLPTRL
                     tblrd*
                                                ; table read here into TABLAT
                     movff TABLAT, FSR1L
                                                ; move adress to pointer, points now to c signum_r(2i)
                     movF INDF1
                                                ; content of c signum_r(2i+1) now in working reg
                     xorWF tmpXOR_lo,w
                                                ; lowest byte [m signum_r (2i+1) XOR c signum_r (2i)]
                     addWFC b_lo,w
                                                ; ADD b with carry
                                               ; IF carrybit =1 ...
                     btfsc STATUS, C
                                                ; then ... add carry
                     incF tmpXOR_ml
                     btfsc STATUS, C
                                               ; IF carrybit =1 ...; then ... add carry
                     incF tmpXOR_mh
                                               ; IF carrybit =1 ...
                     btfsc STATUS, C
                     incF tmpXOR_hi
                                                ; then ... add carry
                     addWFC a_lo,f
                                               ; ADD a, place result in a
                                               ; IF carrybit =1 ...
                     btfsc STATUS, C
                                            , ir carrybit =1 ...
; then ... add carry
; IF carrybit =1 ...
; then ... add carry
; IF carrybit =1 ...
; then
                     incF tmpXOR_ml
                     btfsc STATUS, C
                     incF tmpXOR_mh
                     btfsc STATUS, C
                     incF tmpXOR_hi
                                               ; then ... add carry
term_a2_midlowbyte
                     movF PREINC1
                                               ; content of c signum_r (2i) midlow byte loaded in w
                     xorWF tmpXOR_ml,w
                                                ; midlow byte [m signum_r (2i+1) XOR c signum_r (2i)]
                     addWFC b_ml,w
                                               ; ADD b with carry
                     btfsc STATUS, C
                                               ; IF carrybit =1 ...
                                               ; then ... add carry
                     incF tmpXOR_mh
                                               ; IF carrybit =1 ...
                     btfsc STATUS, C
                     incF tmpXOR_hi
                                                ; then ... add carry
                                               ; ADD a, place result in a
                     addWFC a_ml,f
                                               ; IF carrybit =1 ...
                     btfsc STATUS, C
                                               ; then ... add carry
; IF carrybit =1 ...
                     incF tmpXOR_mh
                     btfsc STATUS, C
                     incF tmpXOR_hi
                                                ; then ... add carry
term_a2_midhighbyte
                     movF PREINC1
                                                ; content of c signum_r (2i) midhigh byte loaded in w
                     xorWF tmpXOR_mh,w
                                                ; midhigh byte [m signum_r (2i+1) XOR c signum_r (2i)]
                     addWFC b_mh,w
                                                ; ADD b with carry
                     btfsc STATUS, C
                                                ; IF carrybit =1 ...
                     incF tmpXOR_hi
                                                ; then ... add carry
                     addWFC a_mh,f
                                               ; ADD a, place result in a
                                               ; IF carrybit =1 ...
                     btfsc STATUS, C
                     incF tmpXOR_hi
                                                ; then ... add carry
```

```
term_a2_highbyte
                     movF PREINC1
                                               ; content of c signum_r (2i) high byte loaded in w
                     xorWF tmpXOR_hi,w
                                               ; highest byte [m signum_r (2i+1) XOR c signum_r (2i)]
                     addWFC b_hi,w
                                               ; ADD b with carry, but carry disapears in black hole
                     addWFC a_hi,f
                                               ; ADD a, place result in a
term_d2
                                                ;... next is d = d xor a \ll 8
                     call compute_dxora
                     movFF d_hi,tmpXOR_hi
                                               ; rotate 8 is actually swapping
                     movFF d_mh,d_hi
                     movFF d_ml,d_mh
                     movFF d_lo,d_ml
                     movFF tmpXOR_hi,d_lo
term_c2
call compute_c
term_b2
                                                ;... next is b = b xor c \ll 7
                     call compute_bxorc
                                                ; now rotate left 7 positions
                                               ; which can be seen as rotate right 1 and byte-wapping
                     bcf STATUS, C
                                               ; prepare Carry flag with 0
                                               ; IF bit 0 of lo-byte
                     btfsc b_lo,0
                                            ; THEN prepare Carry with 1
                     bsf STATUS, C
                     rrcF b_hi
                                               ; rotate through carry
                     rrcF b_mh
                     rrcF b_ml
                     rrcF b_lo
                     \verb"movFF" b_lo, \verb"tmpXOR_lo" ; temporarly save low"
                    movFF b_hi,b_lo
                                               ; swap byte high -> low
                     movFF b_mh,b_hi
                                               ; midhigh to high
                    movFF b_ml,b_mh ; midlow to midlow movFF tmpXOR_lo,b_ml ; low to midlow
                                               ; midlow to midhigh
                     return
                                                ; function d <- d XOR a
compute_dxora
                     movF a_lo
                                               ; load a
                     xorWF d_lo,f
                                               ; d XOR a, result in d
                     movF a_ml
                     xorWF d_ml,f
                     movF a_mh
                     xorWF d_mh,f
                     movF a_hi
```

xorWF d_hi,f
return

```
; function c <- c + d
compute_c
                   movF d_lo
addWFC c_lo,f
btfsc STATUS, C
                    movF d_lo
                                             ; load d
                                             ; ADD c, place result in c
                                            ; IF carrybit =1 ...
                    incF d_ml
                                             ; then ... add carry
                    btfsc STATUS, C ; IF carrybit =1 ...
                    incF d_mh
                                            ; then ... add carry
                    btfsc STATUS, C; IF carrybit =1 ...
                    incF d_hi
                                             ; then ... add carry
                    movF d_ml
                    addWFC c_ml,f
                    btfsc STATUS, C
                    incF d_mh
                    btfsc STATUS, C
                    incF d_hi
                    movF d_mh
                    addWFC c_mh,f
                    btfsc STATUS, C
                    incF d_hi
                    movF d_hi
                    addWFC c_hi,f
                    return
                                              ; function b <- b XOR c
compute_bxorc
                    movF c_lo
                                             ; load c
                    xorWF b_lo,f
                                             ; b XOR c, result in b
                    movF c_ml
                    xorWF b_ml,f
                    movF c_mh
                    xorWF b_mh,f
                    movF c_hi
                    xorWF b_hi,f
                    return
```

B.3 ANSI C

In the C code provided with the submission, we added a function AddSalt(hashState * state, const BitSequence * salt), whose arguments are:

- an initialized state (state)
- a salt (salt) of type BitSequence, long of 128 bits for BLAKE-28 and BLAKE-32, and long of 256 bits for BLAKE-48 or BLAKE-64

The function AddSalt extends the initialization of the hash state by adding a salt as extra parameter. Calling AddSalt is not compulsory; applications that don't use a salt should not call AddSalt. When a salt is required, AddSalt should be called after the call Init, and before any call to Update.

We give our optimized C code computing the compression function of BLAKE-32.

```
static HashReturn compress32( hashState * state, const BitSequence * datablock ) \{
#define ROT32(x,n) (((x)\ll(32-n))|( (x)\gg(n)))
#define ADD32(x,y) ((u32)((x) + (y)))
#define XOR32(x,y) ((u32)((x) ^{(y)}))
#define G32(a,b,c,d,i) do \{ \setminus \}
     v[d] = ROT32(XOR32(v[d],v[a]),16);
     v[c] = ADD32(v[c],v[d]);
     v[b] = ROT32(XOR32(v[b],v[c]),12);
     v[a] = XOR32(m[sigma[round][i+1]], c32[sigma[round][i]])+ADD32(v[a],v[b]);
     v[d] = ROT32(XOR32(v[d],v[a]), 8);
     v[c] = ADD32(v[c],v[d]);
     v[b] = ROT32(XOR32(v[b],v[c]), 7);
   } while (0)
   u32 v[16];
   u32 m[16];
   int round;
   /* get message */
   m[0] = U8T032\_BE(datablock + 0);
   m[ 1] = U8T032_BE(datablock + 4);
   m[2] = U8T032\_BE(datablock + 8);
   m[ 3] = U8T032_BE(datablock +12);
   m[4] = U8T032\_BE(datablock +16);
   m[ 5] = U8T032_BE(datablock +20);
   m[6] = U8T032\_BE(datablock +24);
   m[7] = U8T032_BE(datablock +28);
   m[8] = U8T032\_BE(datablock +32);
   m[ 9] = U8T032_BE(datablock +36);
   m[10] = U8T032_BE(datablock +40);
   m[11] = U8T032_BE(datablock +44);
   m[12] = U8T032_BE(datablock +48);
   m[13] = U8T032_BE(datablock +52);
   m[14] = U8T032_BE(datablock +56);
   m[15] = U8T032_BE(datablock +60);
   /* initialization */
   v[0] = state->h32[0];
   v[1] = state -> h32[1];
   v[2] = state->h32[2];
   v[3] = state->h32[3];
   v[4] = state->h32[4];
   v[5] = state->h32[5];
   v[6] = state -> h32[6];
   v[7] = state->h32[7];
   v[ 8] = state->salt32[0];
   v[8] = 0x243F6A88;
   v[ 9] = state->salt32[1];
   v[9] = 0x85A308D3;
   v[10] = state->salt32[2];
   v[10] = 0x13198A2E;
   v[11] = state->salt32[3];
   v[11] = 0x03707344;
   v[12] = 0xA4093822;
   v[13] = 0x299F31D0;
   v[14] = 0x082EFA98;
   v[15] = 0xEC4E6C89;
   if (state->nullt == 0) {
     v[12] = state->t32[0];
     v[13] = state->t32[0];
```

```
v[14] \stackrel{\sim}{=} state->t32[1];
  v[15] = state->t32[1];
}
for(round=0; round<NB_ROUNDS32; ++round) {</pre>
  G32( 0, 4, 8,12, 0);
  G32( 1, 5, 9,13, 2);
  G32( 2, 6,10,14, 4);
  G32(3, 7,11,15, 6);
  G32( 3, 4, 9,14,14);
  G32(2, 7, 8,13,12);
  G32(0,5,10,15,8);
  G32(1, 6,11,12,10);
state->h32[0] \hat{} v[ 0];
state->h32[1] \stackrel{\cdot}{=} v[ 1];
state->h32[2] \stackrel{\wedge}{=} v[ 2];
state->h32[3] \hat{} v[ 3];
state->h32[4] \stackrel{\wedge}{=} v[ 4];
state->h32[5] \stackrel{\wedge}{=} v[5];
state->h32[6] = v[6];
state->h32[7] \stackrel{\wedge}{=} v[ 7];
state->h32[0] = v[8];
state->h32[1] \hat{} v[ 9];
state->h32[2] \hat{} v[10];
state->h32[3] \hat{} v[11];
state->h32[4] \hat{} v[12];
state->h32[5] \hat{} v[13];
state->h32[6] \hat{} v[14];
state->h32[7] \hat{} v[15];
state->h32[0] \cong state->salt32[0];
state->h32[1] = state->salt32[1];
state->h32[2] \( \) state->salt32[2];
state->h32[3] = state->salt32[3];
state->h32[4] \cong state->salt32[0];
state->h32[5] \stackrel{\triangle}{=} state->salt32[1];
state->h32[6] = state->salt32[2];
state->h32[7] \stackrel{\triangle}{=} state->salt32[3];
return SUCCESS;
```

C Intermediate values

As required by NIST, we provide intermediate values for hashing a one-block and a two-block message, for each of the required message sizes. For the one-block case, we hash the 8-bit message 00000000. For the two-block case we hash the 576-bit message 000...000 with BLAKE-32 and BLAKE-28, and we hash the 1152-bit message 000...000 with BLAKE-64 and BLAKE-48. Values are given left to right, top to bottom. For example

 m_0 m_1 m_2 m_3 m_4 m_5 m_6 m_7 m_8 m_9 m_{10} m_{11} m_{12} m_{13} m_{14} m_{15}

C.1 BLAKE-32

One-block message

IV:								
	6A09E667	BB67AE85	3C6EF372	A54FF53A	510E527F	9B05688C	1F83D9AB	5BE0CD19
Messa	age block a	after paddi	ng:					
	00800000	00000000	00000000	00000000	00000000	00000000	00000000	00000000
	00000000	00000000	00000000	00000000	00000000	00000001	00000000	80000000
Salt a	nd counter	•						
	00000000	00000000	00000000	00000000			8000000	00000000
Initial	state of ν :							
	6A09E667	BB67AE85	3C6EF372	A54FF53A	510E527F	9B05688C	1F83D9AB	5BE0CD19
	243F6A88	85A308D3	13198A2E	03707344	A409382A	299F31D8	082EFA98	EC4E6C89
State	v after 1 rc	ound:						
	E78B8DFE	150054E7	CABC8992	D15E8984	0669DF2A	084E66E3	A516C4B3	339DED5B
	26051FB7	09D18B27	3A2E8FA8	488C6059	13E513E6	B37ED53E	16CAC7B9	75AF6DF6
State	v after 2 rc	unds:						
	9DE875FD	8286272E	ADD20174	F1B0F1B7	37A1A6D3	CF90583A	B67E00D2	943A1F4F
	E5294126	43BD06BF	B81ECBA2	6AF5CEAF	4FEB3A1F	OD6CA73C	5EE50B3E	DC88DF91
State	v after 5 rc	unds:						
	5AF61049	FD4A2ADC	5C1DBBD8	5BA19232	9A685791	2B3DD795	A84DF8D6	A1D50A83
	E3C8D94A	86CCC20A	B4000CA4	596AC140	9D159377	A6374FFA	F00C4787	767CE962
State	v after 10 i	rounds:						
	BC04B9A6	C340C7AC	4AA36DAA	FDB53079	OD85D1BE	14500FCD	E8A133E1	788F54AE
	07EEC484	0505399D	837CCC3F	19AD3EE7	9D3FA079	FA1C772A	FODFD074	5C25729F
Hash	value outp	ut:						
	D1E39B45	7D2250B4	F5B152E7	4157FBA4	C1B423B8	7549106B	07FD3A3E	7F4AEB28

Two-block message

1	١	,	
1	١	ν.	

6A09E667 BB67AE85 3C6EF372 A54FF53A 510E527F 9B05688C 1F83D9AB 5BE0CD19

First compression Message block after padding:

	00000000 00000000								
Salt an	Salt and counter								
	00000000	00000000	00000000	00000000			00000200	00000000	
Initial s	tate of ν :								
	6A09E667 243F6A88	BB67AE85 85A308D3	3C6EF372 13198A2E	A54FF53A 03707344	510E527F A4093A22	9B05688C 299F33D0	1F83D9AB 082EFA98	5BE0CD19 EC4E6C89	
State ν after 1 round:									
	CC8704B8 01A455BA	14AF5E97 43BAAEC3	448BD7A4 CO7C7DEC	7D5ED80F 4C912C63	88D88192 6F8CDFEC	8DF5C28F 87FD02E0	B11E631F D969B7B1	0AC6CEAB B74125B6	

State v after 2 rounds:

D7ED8FC3 CC0A55F2 24014945 38A9D033 8DA19E93 9B91D76A 18E0448C C10A0DF6 FB350B3C D894B64E F1B35175 D0DFF837 54E0DF8F B3131C53 64BCB7A4 819FDFEA

State v after 5 rounds:

6BB8EAA1 FB2D35B9 F1C87115 8CCED083 C3CCF47F EC295B60 18CF9A21 DC2AC833 1F87FBA1 759AE5F0 EE2F791D 11410F9F 46C442D0 EC5BE440 DC9ED226 97E6E8BC

State v after 10 rounds:

58B76F7A 24300259 EA5BAEE6 7ABECB5C BEAAOC3C 38251BB6 F0D337AF FF985D99 527E3C0C 4EBFC5FA BF73D485 8B538346 03C56421 D1B9147E 63662E6C 70E9E8B2

Intermediate hash value

60C0B511 D1E86926 69468911 54A2BD20 EC613A62 72996744 8C36C068 D4917832

Second compression Message block after padding:

Salt and counter

Initial state of v:

60C0B511 D1E86926 69468911 54A2BD20 EC613A62 72996744 8C36C068 D4917832 243F6A88 85A308D3 13198A2E 03707344 A4093A62 299F3390 082EFA98 EC4E6C89

State v after 1 round:

2A12A61C 97455E40 71CEADC4 910B1078 420B2A13 EB18D4FC 179C8D8F 32115CDC 09A6088F 6698DD12 B7CD9DED 29E4EBE7 660D3499 75061D15 52848DFD FC099457

State v	after 2 ro	unds:						
	F4C6263D 211995BC	7327094B CE94B418	D139C80D 5391B476	18A95331 6D480D9D	6211D241 70988FB3	1BA339FA 114F5AF1	4F059AB4 8648B874	AA1580E9 4F87AF38
State v	after 5 ro	unds:						
	ECFEE77A 27B8D497	1F878081 30FB68D3	339A7A59 0ACF6405	D4CED068 524F093A	73649B08 14E97D67	A3ACE1DA DCC7C7B0	A0B085A5 98EA099A	22CCBB53 A41ECBCA
State ν after 10 rounds:								
	74CBFCFA 9E68CD63	BC46AECD AEB60243	8835BA12 C3592B10	FA9767EE B979EC7A	E1AAF6A5 B6AD289C	2394033A 58A2B983	D433008D 272EEF06	897E05BB 4BF407E4
Hash value output:								
	8A638488	C318C5A8	222A1813	174C36B4	BB66E45B	09AFDDFD	7F2B2FE3	161B7A6D

C.2 BLAKE-28

One-block message

IV:								
	C1059ED8	367CD507	3070DD17	F70E5939	FFC00B31	68581511	64F98FA7	BEFA4FA4
Messa	age block a	after paddi	ng:					
	00800000	00000000	00000000	00000000	00000000	00000000	00000000	00000000
Calt a			00000000	00000000	00000000	00000000	00000000	00000008
Sall a	nd counter							
	00000000	00000000	00000000	00000000			8000000	00000000
Initial	state of ν :							
	C1059ED8	367CD507	3070DD17	F70E5939	FFC00B31	68581511	64F98FA7	BEFA4FA4
	243F6A88	85A308D3	13198A2E	03707344	A409382A	299F31D8	082EFA98	EC4E6C89
State ν after 1 round:								
	04027914 481423A7	24CFDD6B 2F45B4F9	7D33F394 21C35492	12CBCC67 50FB35FE	2DE38C62 1255AE24	6664F3D3 DFF2A626	1D8D68FC 9240D453	D6CD0B0B E8530B9D
0			21035492	30FB35FE	1255AE24	DFF ZROZO	92400433	E0030B9D
State ν after 2 rounds:								
	9FB36742 36EF0086	31BC5AC2 38DFA9E5	064D4095 A67CC4B5	4A2260B2 20963EEB	C12165D2 F2821838	00D0EE58 D01907D2	AD1D8245 7D15E12D	4F7B0F17 9B9EF864
0, ,			A07 CC4B3	20903EEB	F 2021030	D01907D2	70136120	9D9EF004
State	ν after 5 rc	ounds:						
	AAB629F7 93068AB9	16DE3E4A 67EA727C	5E78A622 5EC4C9A9	257EBE3C 7212CD6A	8669EA65 7F90526F	99D687FD 6E8952F4	A632EA5E 70E30791	511B1C46 16C1EBD8
0			5EC4C9A9	72120D6A	/F90526F	0E0952F4	70E30791	IOCIEDDO
State	ν after 10 ι	rounds:						
	C9E1652F 62A1B43D	BA9E5BDE E2D6F00A	660E702E 67AAA716	67FC6579 E006A66D	BE6B4C7F 95556F38	F5F0749A 8145A426	1DFE158F 1EC4DE7E	3B49131F FC75FF74
			OTHANT 10	FOOOROOD	33330F30	01408420	TEC#DE/E	1010114
Hash	value outp	ut:						
	6A454FCA	6E347ED3	31D40A2F	70F49A2D	D4FE2876	1CEDC5AD	67C34456	

Two-block message

i	١	/-	
-	١	/	

C1059ED8 367CD507 3070DD17 F70E5939 FFC00B31 68581511 64F98FA7 BEFA4FA4

First compression	Message block after padding:
LII2f COIIIDI 6221011	Message block after padding.

	00000000	00000000	00000000	00000000	00000000	00000000	00000000	00000000
Salt an	d counter							
	00000000	00000000	00000000	00000000			00000200	00000000
Initial s	state of ν :							
	C1059ED8 243F6A88	367CD507 85A308D3	3070DD17 13198A2E	F70E5939 03707344	FFC00B31 A4093A22	68581511 299F33D0	64F98FA7 082EFA98	BEFA4FA4 EC4E6C89
State v	after 1 ro	und:						
	E5B52991 8BC4F63C	1FBB7ECB C1C7FE8C	F7350E64 1FA6AE53	0C8D11C6 EE4DC034	148B1E94 87863887	7C688FED 2D70805B	C8FEEE1B 4FA9A232	4046AC6E D9860F12
State v	State v after 2 rounds:							
	2F3A90E3 6E8F7EEB	EBBBC331 115D1FD6	5737A2D1 43387C5F	6480F282 FFB59797	DB471183 F8663D1A	43014ABD D5FA0EC9	88924F03 0C0ED9E5	5160CB72 8579D4A6
State ν after 5 rounds:								
	F729608D 06F32665	8119B461 23B502C7	E62F4D54 FEDC26FC	7889D045 CEFD14A6	838FBD7D DAD6B58F	1A1E5618 4DCAOD19	8728C02B 31D904CB	E973E337 3C7E2160
State v	State ν after 10 rounds:							
	D3465C90 7B80826F	9AF58DB6 21577A7A	77044D06 CE253568	8782E7B8 1B6A082B	F5C3F50A D5E512E2	78A3A751 E213D8E0	D7923EF6 F39651A7	647B8D32 F9FDAE6E

Second compression Message block after padding:

Intermediate hash value

Second	Second compression Message block after padding:							
	00000000 00000000	00000000 00000000	80000000	00000000 00000000	00000000 00000000	00000000 00000000	00000000 00000000	00000000 00000240
Salt ar	nd counter							
	00000000	00000000	00000000	00000000			00000240	00000000
Initial s	state of ν :							
	69C34027 243F6A88	8DDE22CB 85A308D3	8951A579 13198A2E	6BE6B6AA 03707344	DFE6ECD9 A4093A62	F2E86AA0 299F3390	40FDE0F6 082EFA98	237C6CF8 EC4E6C89
State ν after 1 round:								
	215AEB86 7F047CFA	8A40E284 BCBFA0C8	8889C5CF 8E907E6C	3A7A93F9 582C5CC4	3ECC4417 C7C016E8	4EB11689 696F917E	3B06106F 0AF46854	0092D184 929FD9AB

69C34O27 8DDE22CB 8951A579 6BE6B6AA DFE6ECD9 F2E86AAO 40FDE0F6 237C6CF8

State v after 2 rounds:

998F9380	6D6C16FD	79CE8034	65B3E4A4	459C22CC	3B8EA998	35638BB5	D9F54BB2
A3C7177D	A3E59D0B	A059BBAF	C62D9E5A	B1A2808E	9032CCCB	B36DB002	ECDC6D0D

State ν after 5 rounds:

2E967A8A 56885CE5 8218AB56 CFBA4356 32627515 913CB1C0 F480A1AE B524AE3A 643AE882 419A50AA 74CDF767 CFC40BDF 2FDDA24A 42651292 2B4A4CE2 B7B83356

State v after 10 rounds:

2C975117 5D90EBA5 78A0F5C4 FB0EDE6F E88CE2F8 03206935 CD05A414 05F47C03 2B9CC580 2EE07DFA A110229E DCE37F4B 4E31D239 23EC233D D697DF5B 86F74FCC

Hash value output:

6EC8D4B0 FEAEB494 50E17223 4C0B178E 795BDC18 D22420A8 5B6F9BB9

C.3 BLAKE-64

One-block message

Message block after padding:

00800000000000000	00000000000000000	0000000000000000	00000000000000000
0000000000000000	0000000000000000	00000000000000000	00000000000000000
0000000000000000	0000000000000000	00000000000000000	0000000000000000
0000000000000000	0000000000000001	00000000000000000	8000000000000000

IV:

6A09E667F3BCC908	BB67AE8584CAA73B	3C6EF372FE94F82B	A54FF53A5F1D36F1
510E527FADE682D1	9B05688C2B3E6C1F	1F83D9ABFB41BD6B	5BE0CD19137E2179

Salt and counter

Initial state of ν :

6A09E667F3BCC908	BB67AE8584CAA73B	3C6EF372FE94F82B	A54FF53A5F1D36F1
510E527FADE682D1	9B05688C2B3E6C1F	1F83D9ABFB41BD6B	5BE0CD19137E2179
243F6A8885A308D3	13198A2E03707344	A4093822299F31D0	082EFA98EC4E6C89
452821E638D0137F	BE5466CF34E90C64	COAC29B7C97C50DD	3F84D5B5B5470917

State v after 1 round:

98957863D61905B3	2064357139454E43	391FB64BD757FB63	A77C0E00BBE362B5
86D4B6C41F60C7E1	823F30053BEB147C	68E6FC038D3B0B70	D93165F3477733DF
DED9D48A51DDE68F	3B73BB8B500C22B1	03F92332A668036B	E2F0B698EA636BB9
A40103908A3FD2AF	0166134D1447C604	RFRC229C63F28R76	0245006146695434

State ν after 2 rounds:

84DAC4B310F8B76B	01CE15A3AA8D8B2E	F12C708C9D10A8B0	778C288779642198
13D4F878F30C3F5E	5B049744B1932015	OFCFCODEE2COF4AO	80B67926A85E5AD8
8D0E3FB6C987BE2B	A1E68630BE9171C7	06D755881837E80F	B8729CFE5D112FA0
9226C2A7D8AD1F76	8265C86D8C126BC1	COBFC6FEEOCFF19B	E48FA8828EEC436A

State v after 5 rounds:

EFD689A66BDC0A95	2253DDE0CB058FFC	886B8A405AE244FA	CA317DFE42522691
FB5123461DF359E7	17EFB7C5FD09F586	8E07FE0BD4918C29	E3AE0ACDF25D6303
6D4719E51F4A0833	27218B65BD7D4BC0	9227B3EA1497AD64	72B2C922552B72F9
855C5D1C44DD57A4	FC1340AE55773E39	03B57F827BE2F1CD	B43F42F4AA368791

State ν after 14 rounds:

1C803AADBC03622B	055EB72E5A0615B3	4624E5B1391E8A33	7B2A7AA93E27710A
F7EA864E4D591DF7	34E2FF788DBD71A7	01D13A3673488668	390D346D5CB82ECF
OOD6AC4E1B3D8DEO	58CD6E304B8AD357	33E864217D9C1147	C9C686A43790D49F
8C76318C3B9E3C07	20952009E26AE7A1	E63865AEC6B7E10C	2FAFFDCB74ADE2DE

Hash value output:

765F7084548226C3	E6F4779B954661DF	49A272E2BA16635F	17A3093756AA9364
2A92E5BDDB21A321	8F72B7FD44E9FA19	F86A86334EBEDA0F	4D4204BF3B6BED68

Two-block message

IV:

6A09E667F3BCC908	BB67AE8584CAA73B	3C6EF372FE94F82B	A54FF53A5F1D36F1
510E527FADE682D1	9B05688C2B3E6C1F	1F83D9ABFB41BD6B	5BE0CD19137E2179

First compression Message block after padding:

0000000000000000	00000000000000000	00000000000000000	00000000000000000
0000000000000000	00000000000000000	00000000000000000	00000000000000000
0000000000000000	00000000000000000	00000000000000000	00000000000000000
0000000000000000	0000000000000000	0000000000000000	0000000000000000

Salt and counter

0000000000000000	00000000000000000	00000000000000000	00000000000000000
00000000000000400	00000000000000000		

Initial state of ν :

6A09E667F3BCC908	BB67AE8584CAA73B	3C6EF372FE94F82B	A54FF53A5F1D36F1
510E527FADE682D1	9B05688C2B3E6C1F	1F83D9ABFB41BD6B	5BE0CD19137E2179
243F6A8885A308D3	13198A2E03707344	A4093822299F31D0	082EFA98EC4E6C89
452821E638D01777	BE5466CF34E9086C	COAC29B7C97C50DD	3F84D5B5B5470917

State v after 1 round:

1BE45837F23BAEE5	2111F54A79AD333D	F51F6F4BDBDACC64	BFD3AF47522BA647
3CBD1A03BABEE0B1	4C1679E18847BED0	65375DDA217AF370	FC804555EA9C61C0
13DCA8E50FCBEEA2	A028A1030A7F2907	A8486683A019458C	6F50BBC1BAAD52D1
26FF0C474E8A8E46	3661DBA5D8ADCE89	FB6E1530F3FA0CD2	29F3D982476D1C5B

State v after 2 rounds:

078A7F4AB38B51A3	3CC938D334F088AE	C9688433013EB5F4	963A2028D731F262
A2E4F2F9127A623E	7DF540DFFEC115F7	539403CCFF3E7EDA	4039A268638B91E7
6DE0D9BF908EF408	D9747550EADAF1B2	5CBEB17148553D5C	CC40FD3E15DD6C42
528F6D54B521156E	CE320314E7255341	C374721DDC0FEEB2	F64047D64AED39A9

State v after 5 rounds:

7CE663EFB2F3997D	CA831A13AE1ADEA2	1B489B08D9C77613	8449E1F48BF74A4A
D7F36F5DAD19B6F0	1B79A03B9DADCC93	OC5A6120750E5B4A	4D74C0055FEA4D29
91ECB03DDFB95F46	D12929425D257265	4436F30BA8FDA059	8F5EA5D22A3CFC07
1591886653094950	A98739E101B44D3A	78556C535F2905F2	E5BC8EDDAC0176DF

State v after 14 rounds:

BAE5B20438E	BD1AE I	FB9EB556D67BE6CD	1DD32AA12CB2C411	42374BFECE90FA65
807E55B1992	34ECC	7FC73B526FADC9D8	760B6B884BA1B098	B77D0E14CCB094DD
FB079B4D090	DA172 I	EE56FD3B622F28AC	A4C9C6924B60C4B9	244E57A15B596644
7C86CAACE54	A8E3E	71782EF1771E5ABA	5FCE8F0139CBA368	D3F1A57A2BD841F4

Intermediate hash value:

2BEBCF2EC29AB9D4 AEAFE6E8309E695A 85741F419946F883 C336E965CAD4AAD0 ADF6CD62D18F4223 95BA7D2F338DFF7D 36463D22892BAE9B 3F6C6677F416F450

Second compression Message block after padding:

00000000000000000	00000000000000000	80000000000000000	0000000000000000
0000000000000000	00000000000000000	00000000000000000	0000000000000000
0000000000000000	00000000000000000	00000000000000000	0000000000000000
00000000000000000	00000000000000001	00000000000000000	0000000000000480

Salt and counter

Initial state of ν :

 2BEBCF2EC29AB9D4
 AEAFE6E8309E695A
 85741F419946F883
 C336E965CAD4AADO

 ADF6CD62D18F4223
 95BA7D2F338DFF7D
 36463D22892BAE9B
 3F6C6677F416F450

 243F6A8885A308D3
 13198A2E03707344
 A4093822299F31D0
 082EFA98EC4E6C89

 452821E638D017F7
 BE5466CF34E908EC
 C0AC29B7C97C50DD
 3F84D5B5B5470917

State v after 1 round:

 97B7744F66047D30
 EFAF6C7255A85A64
 18269E18102C7DF0
 5845FCE8352347AA

 33945C40520094E4
 BF2E239191F3FB2A
 F52AA83F401E1C94
 03D39EF6D699D428

 C9C5F695FF595911
 BA2CB996500E645A
 043F4721E6185DC6
 F06941D9A4AE3838

 45F73F26426EDC75
 9C1FDEEE8C3B71F6
 E362AD2A84BA1C65
 972A9B18D218E63C

State v after 2 rounds:

77DDF1D318481AF5 0E5BB7B53A077AB3 52AC32E7E020E8C4 9F2D720DFA259B0E
AA8C0FD13D1AC0EC 85AC17EB7D90CB3C 45C7BAC2500D182B F70ABDEDE7FBE95B
4B8145BC80391D37 8CE035CEB9332CCE 5160F2E0762575C9 5F14547FC0B45158
B8033BABB00BB947 4690BE32AC7037B1 A8841F193796A0AF E0C40F4CDA85533A

State v after 5 rounds:

4E1FE57385697E55815DEE13C3C990D8AAB9BC1621BFDB4C24308C06892728BEC72F23D392287B055CAB7BB581F70C1FADA9296C20920C0232CBBC0000666FE8AAE844890FC188D6FFAA213A3CC310DFECA6E32297722DC89C5D5C2CCF01C274AF2A09A3721A949B6C3461C3134774B648C942D2E0B00355D5BF25B37AA44AE1

State v after 14 rounds:

 60EF7F97E6FE03C5
 EB78F18831CFFFE8
 1207B65336348F8E
 D380A238CA002C04

 87CFE47BA3E06881
 568BE33B0D9007D7
 5D4147CBD6987380
 504CD06EA90E16AF

 A1B38091204C9B14
 3424EFBEE7293F03
 2C9CF1CDFA356568
 A7A86D768E2B3CF1

 19F87A0EB186D235
 7158735578B32859
 C99F5DEF5FE6170F
 0A07E5F6BF1273C1

Hash value output:

EAB7302804282105 71F3F8DEE678A9B1 BBEF58DF55471265 B71E262B8EFFBA25 33C15317C3E9F897 B269ED4146AED0F3 A29827060055CA14 652753EFE20A913E

C.4 BLAKE-48

One-block message

Message	block	after	paddir	na:
				9

Message Di	ock after padding	•		
	008000000000000 0000000000000000 0000000	0000000000000000 0000000000000000 000000	0000000000000000 0000000000000000 000000	000000000000000 0000000000000000 000000
IV:	CBBB9D5DC1059ED8 67332667FFC00B31	629A292A367CD507 8EB44A8768581511	9159015A3070DD17 DB0C2E0D64F98FA7	152FECD8F70E5939 47B5481DBEFA4FA4
Salt and co	ounter			
	000000000000000000000000000000000000000	000000000000000000000000000000000000000	0000000000000000	0000000000000000
Initial state	of ν :			
	CBBB9D5DC1059ED8 67332667FFC00B31 243F6A8885A308D3 452821E638D0137F	629A292A367CD507 8EB44A8768581511 13198A2E03707344 BE5466CF34E90C64	9159015A3070DD17 DB0C2E0D64F98FA7 A4093822299F31D0 C0AC29B7C97C50DD	152FECD8F70E5939 47B5481DBEFA4FA4 082EFA98EC4E6C89 3F84D5B5B5470917
State v after	er 1 round:			
	5B063A05F1A479BB C0836949C0FA750A 5EB10A738BF891EE C83CF461EDC79B6D	82CA717B7A4F6F94 99FD9AA2E726BF09 3DF23E84618C549F 8FF3FB919A781656	4F58DFBDAB593FFB 32F52E2CBFC45A64 F2C230E414F34299 9BE2FD02DFE1B98A	F826C578573BEC7E 80686C4AE126CDA9 9191632BEE7EE45E 5B64934E1FE8370D
State v after	er 2 rounds:			
	5B2B57C1586FEEA6 9E3CD39F1C1868DA B9F9689AFC6AEDA6 F7BA66DC1AEB284C	7413D0FE48C32BE2 A4D8C74D2A7AA0F5 EBC0E49C45A1E9AA 9C362FBCE59789D9	535CA6F699C38D80 7524F4211494EF12 260D24A2D818CB43 74B3B2650C513D2C	BBEEOCOCBD530269 A94A548795A319EC BA3914617A2D98EC D53EB118A489C053
State v after	er 5 rounds:			
	4292009F26C4CAA5 7ECAF3B6BC20CFD7 A0E941F5B18548FA CB09E853BA91C13D	17DF7CF80E7A6542 00D47510478C61B9 BFCB96FC91F31717 FD46E7FE45AA85E3	24CA7FE6607B8393 F1A2F95870EAF7B0 4B9F4584075D75C4 CE6E1C891FFAAEF9	C91DDCA2AFECD146 52AD845DA7D26918 BF9C0EE7E53657FF 2C9E50427598264A
State v after	er 14 rounds:			
	1DD69F386C168B30 94ABF0918D4B9749 2EC5D56650765851 88EA30691A1873AA	EB4B1AD311C7C265 6A59118B73AB159B B84BF78188E22A8D DABF685D0556D4AF	42044AA20151C2A0 56EE21C11395B066 5149DF33128FAAC1 51168CA096930C62	1BD8CBE637DFB25D 00BB340A4C94C03B 8E52CD242ADB8EA8 E42652FFB6D559CF
Hash value	e output:			
	F8A8D703FD654DB9 7B72E69F6893EFD2	319AC478AF593DEF 3E5233511EA5D425	821494CB23AEB576	80A5EA1AEA0A65CC

Two-block message

IV:

CBBB9D5DC1059ED8	629A292A367CD507	9159015A3070DD17	152FECD8F70E5939
67332667FFC00B31	8EB44A8768581511	DB0C2E0D64F98FA7	47B5481DBEFA4FA4

First compression Messag	зе віоск а	fter padding:
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	000000000000000 0000000000000000 000000	000000000000000 0000000000000000 000000	000000000000000 0000000000000000 000000	000000000000000 0000000000000000 000000		
Salt and	counter					
	000000000000000 00000000000000400	000000000000000000000000000000000000000	00000000000000000	0000000000000000		
Initial state	Initial state of v :					
	CBBB9D5DC1059ED8 67332667FFC00B31 243F6A8885A308D3 452821E638D01777	629A292A367CD507 8EB44A8768581511 13198A2E03707344 BE5466CF34E9086C	9159015A3070DD17 DB0C2E0D64F98FA7 A4093822299F31D0 C0AC29B7C97C50DD	152FECD8F70E5939 47B5481DBEFA4FA4 082EFA98EC4E6C89 3F84D5B5B5470917		
State ν after	er 1 round:					
	3BBF567D6D8E7C9A 1F7BFE2284B78162 ADA82F0DD0769947 C802F0CF294F6269	826AB1796F4B2F2A E1F997F6B243CD2A C23086272083F261 C6F36399DF7E1E35	D3589AB1A73A76FB 70B6BA23B832F52D F6A871C70393F9FA 8F20EDDF0BA7D74A	7FFB66FFAAA078B4 B5418F66EC6D2031 8D515B125606EADA DE4472F1D1506E6F		
State v after	State v after 2 rounds:					
	EA85A242A7F6CFCE 5D085C4433F1929C F4A2235795910F0F 48D6E244313C9D0C	89A54C23487CA8BF 8134381EEE29381F 58AD370D224CB9B0 D079DE27CBA8F3C8	5C8893D38EF63BF3 36505EC762DAB50C 47D1E79A61966B91 DD134C5A6384EFAC	46B087AA28D56BE5 D71519E8814D4E39 0563F8E3BA681DBD 7E27A4AC04CF472D		
State v after 5 rounds:						
	802C1F2E2198AE80 D88DF0E4BFC0ADAB 014C1C71F0918E4D 0D2FB5DCD1ADE0AE	EE5B58BB836A1D70 7871BB15B4555CAB EA826F742DAA21D0 7C972BBFEF957FB5	8157B2DA7FB7781D F89864B706E11F5F 33C03F7DFB0166DC 7D874F206DD2E3FB	9295E0C42DC728FC F01F54F3CB2B4E5F 11442F58CFC88765 8CFE8958C6233803		
State v after	er 14 rounds:					
	48D2ABEEC2D71CC5 AF9FDE1EE3CAD40D 12D0217D0E74E5B1 16DAC45878471174	453ACF7BB753BBF1 C661F45A89950ADC CC7BD5E254C52B17 CDAE5B050C98E92A	8AD951B5121E15F2 843A9EE5D8169BD5 8636BF1D9B6E636B 121004668DBAB665	6D70D249D39A715A C74BC1121B511E1A E5FDF466195146E0 AEF35F816CEA29F2		
Intermediat	te hash value:					
	91B917CE0DA667AC DE763C21644DCE48	EBDB33B3D5EA45E1 857BE5D8ED55F6E7	9DB6EFF2B900AB8E 4D26B48E3155A217	9DA2CAF73DC56E83 2E0DD68EC941784C		
Second co	mpression Mes	sage block after p	padding.			
	00000000000000000	000000000000000000000000000000000000000	80000000000000000	00000000000000000		

0000000000000000	0000000000000000	8000000000000000	0000000000000000
00000000000000000	0000000000000000	0000000000000000	0000000000000000
00000000000000000	0000000000000000	0000000000000000	0000000000000000
00000000000000000	00000000000000000	00000000000000000	0000000000000480

Salt and counter

00000000000480 000000000000000

Initial state of ν :

91B917CE0DA667AC	EBDB33B3D5EA45E1	9DB6EFF2B900AB8E	9DA2CAF73DC56E83
DE763C21644DCE48	857BE5D8ED55F6E7	4D26B48E3155A217	2E0DD68EC941784C
243F6A8885A308D3	13198A2E03707344	A4093822299F31D0	082EFA98EC4E6C89
452821E638D017F7	BE5466CF34E908EC	COAC29B7C97C50DD	3F84D5B5B5470917

State *v* after 1 round:

EB5305AF9C675316	B04F4367EF5BCB01	C5ACFFF4A502B3AC	7B1494BE21EA8AEC
EFC2114AF5B89E14	8C5D51A5085E8343	FB3871A4E93CDC4C	730A928E549F309C
EB5B62A3636B5994	380D6D5F3BE6DE51	OC3A9D08903CE741	C89B96FA0C4FE476
5406B1EE5E8E0B04	DE7BCC2A14B5687D	189291CFE98DD45F	CCOAEDF772238F5A

State ν after 2 rounds:

EDDD82F01BAC0561	4CFDCDFFA77330A4	A3BEC55427F66DD0	E61E7A01F5B44065
697C76A05841756C	C4238D4E0E4F480C	1924ABE4F334FCE1	4410660CC930607C
4CD8F10D348336C4	8A2C792E6B6607D4	FC362721166BF27C	BF00A632885CC7ED
1B470C101AA73F07	F21D3F3E6C497536	C6A24BD8C6E548A5	0C9F27FDC4AA89C1

State v after 5 rounds:

OB54F86A35B74457	A4315CE1B09ADE8D	E3078EA3D51F8EA4	453748C8FEDC0071
EADF5CBCC39D038D	D9763C0B677A4587	B0EBA224DEE4E974	AFEA28B0B8AAE56C
BB57DFD78B8B4D38	7B04C7FDE21E1FB1	5FE3B5E55E53DA1D	9483FC16047631D4
437715901F3DBBAF	34AC592C780C505B	0475414152111284	80397DEF4F32B2BF

State ν after 14 rounds:

757F77BF12F5C1B0	223D06220DB9BFF2	330D25F2DA9321D4	CC96ECE63FA108EA
TOTT THE IZE COLDO	ELODO O EL O BODI I E	CCCDECT EDITOCETD I	OCCOPORATION INTO PRINCIPAL PROPERTY OF THE PR
3BCB8A5F730CE929	9A760947DC3E64DE	5790F83BFC764982	ADDDA3E22C5AB3C5
SECEONSF / SUCESZS	38100341DC3E04DE	3190F03BFC10490Z	ADDDA3E22C3AD3C3
2CC451168EAEDAOF	5C335D58949ACF0D	89406B7B3F0A86C0	F814998AD3057F48
200451166EAEDAUF	50335D58949ACF0D	89406B1B3F0A86C0	F014990AD3U5/F40
070E440047DC0EEE	000744744004046	4 F A 2 F C O F 2 F D 0 D 0 F 0	0D0DE0040E000E07
073E119817B69FF5	83F/A1/41EE1F446	15A3F6053FD0B9F0	0B2BE29A95030597

Hash value output:

C802316791FD7C13	95D568C94CC9351E	27FBA17B5C990C9A	A920BF9BD1611921
E283A7E600F7B894	9CFA4DEB2F8A667F		